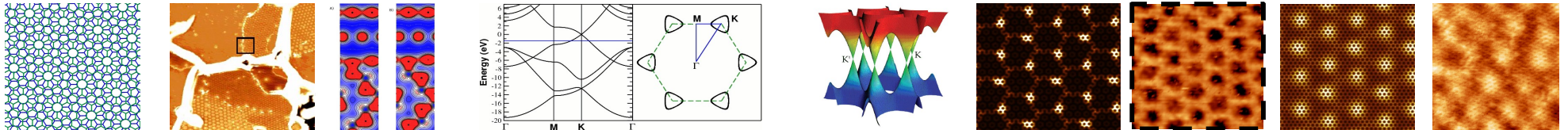


Structure électronique d'un biplan de graphène couplage ab initio – liaisons fortes

L.Magaud

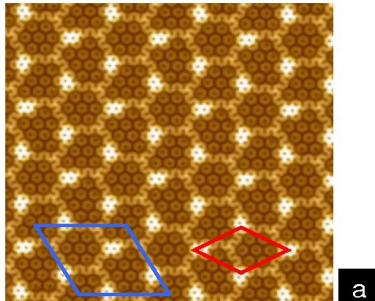
Institut Néel, CNRS-UJF, Grenoble,

France



1. Interface graphène – Face Si de SiC

- Données expérimentales
- Plan tampon



$6\sqrt{3} \times 6\sqrt{3}$ R30 (>1300 atomes)

approche DFT (VASP)

potentiel classique EDIP : C sp^2 et sp^3 + Si-C et C-C

2. Biplan de graphène tourné

- Données expérimentales
- Calculs ab initio
- Liaisons fortes

3. Conclusion et futur : croissance

Introduction : Methods - technical details

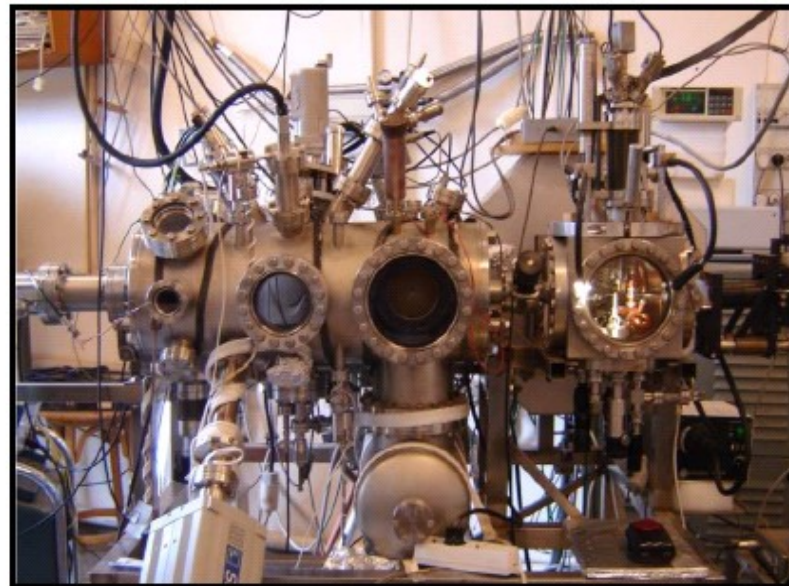
DFT calculations:



DFT + GGA
pseudo potential + plane wave
large supercell (>1200 atoms)

F.Varchon, F.Hiebel, L.Magaud
IN and PHYNUM

Scanning tunneling microscope :



Home made UHV- STM
6H SiC (0001) and (000-1),
n doped

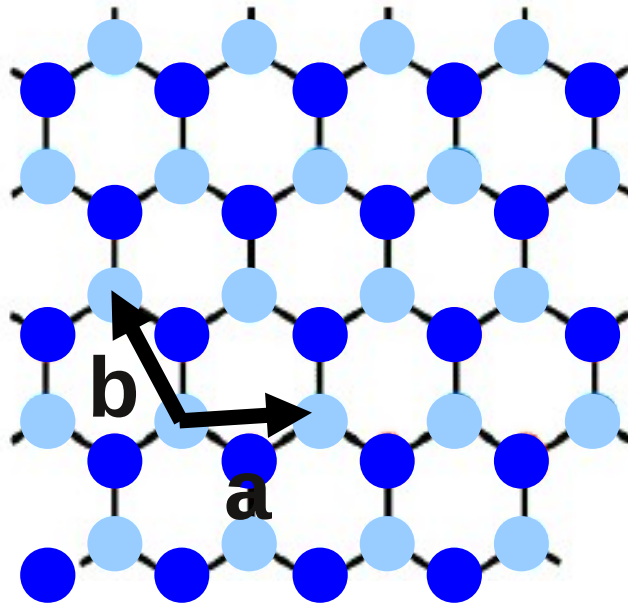
Si flux at 850 °C
progressive annealing
(900 -> 1100 °C)

F.Hiebel, F.Varchon,
P.Mallet, J.-Y.Veuillen

Le graphène :

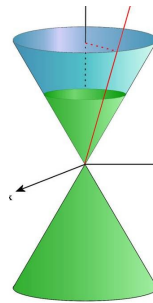
exfolié (Geim Novoselov, Kim)
sur SiC (de Heer)
sur métaux

1 plan de C en réseau nid d'abeille

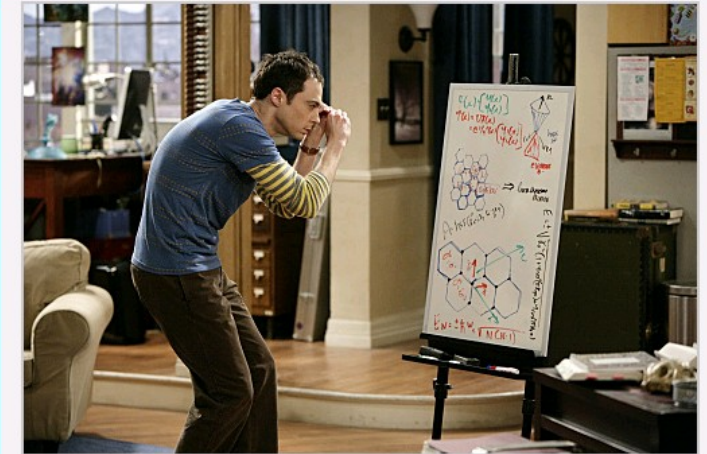


$a=b,$
 $\theta=120^\circ$

Réseau de Bravais hexagonal

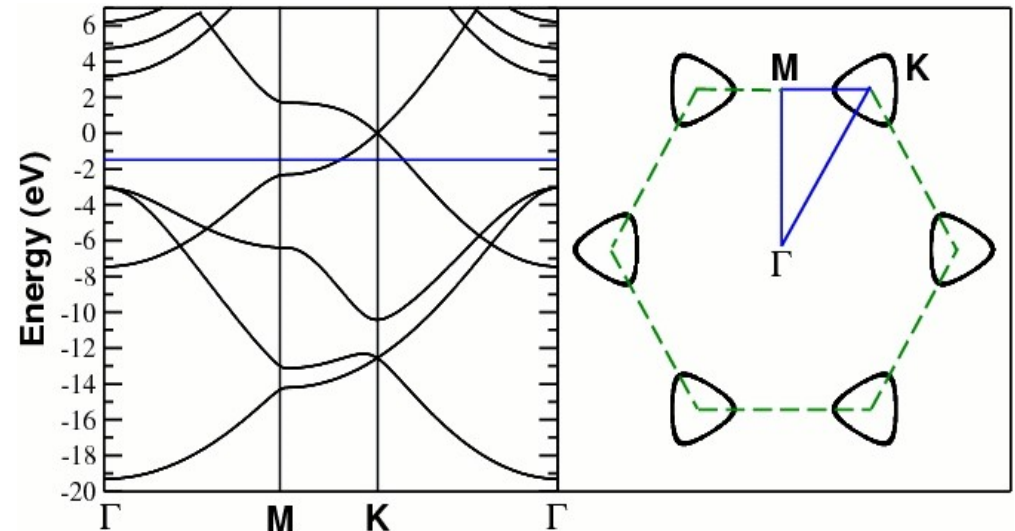


The Einstein Approximation #1424

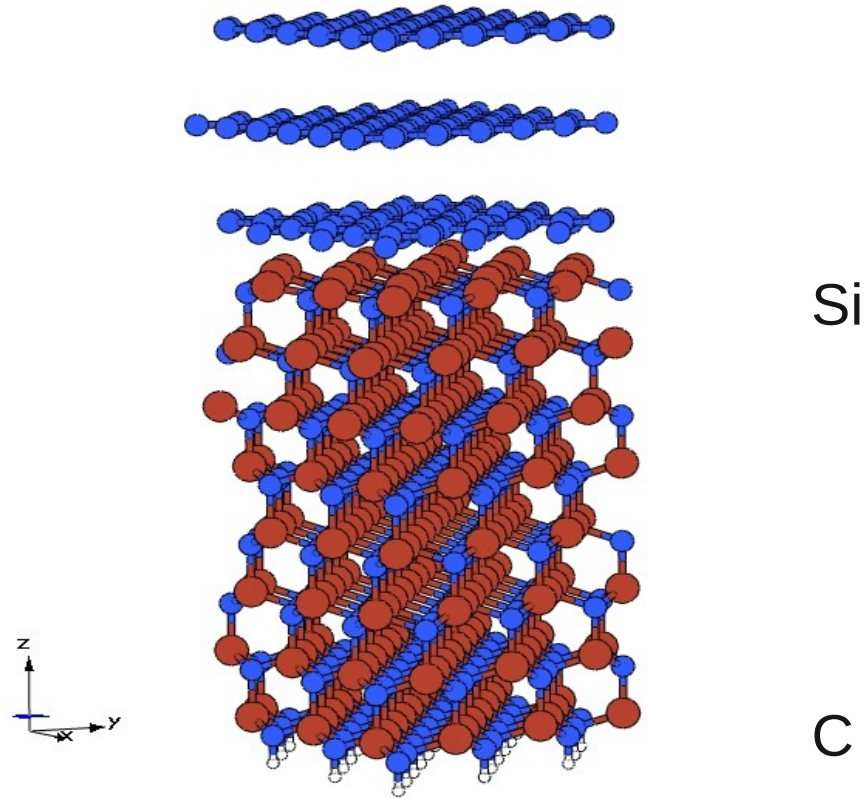


'The Einstein Approximation' - Season 3, Episode 14

Sheldon's search for the answer to a physics problem leads him to work at the Cheesecake Factory with Penny.

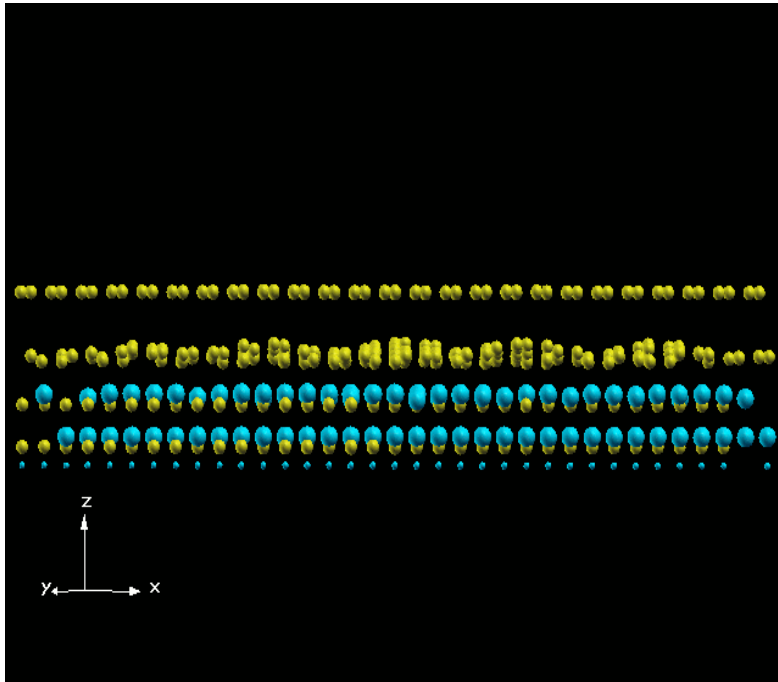


Faces polaires des polytypes hexagonaux de SiC



Si face : strong interaction with substrate => buffer layer

Common cell graphene – SiC
 $6\sqrt{3} \times 6\sqrt{3}$ R30

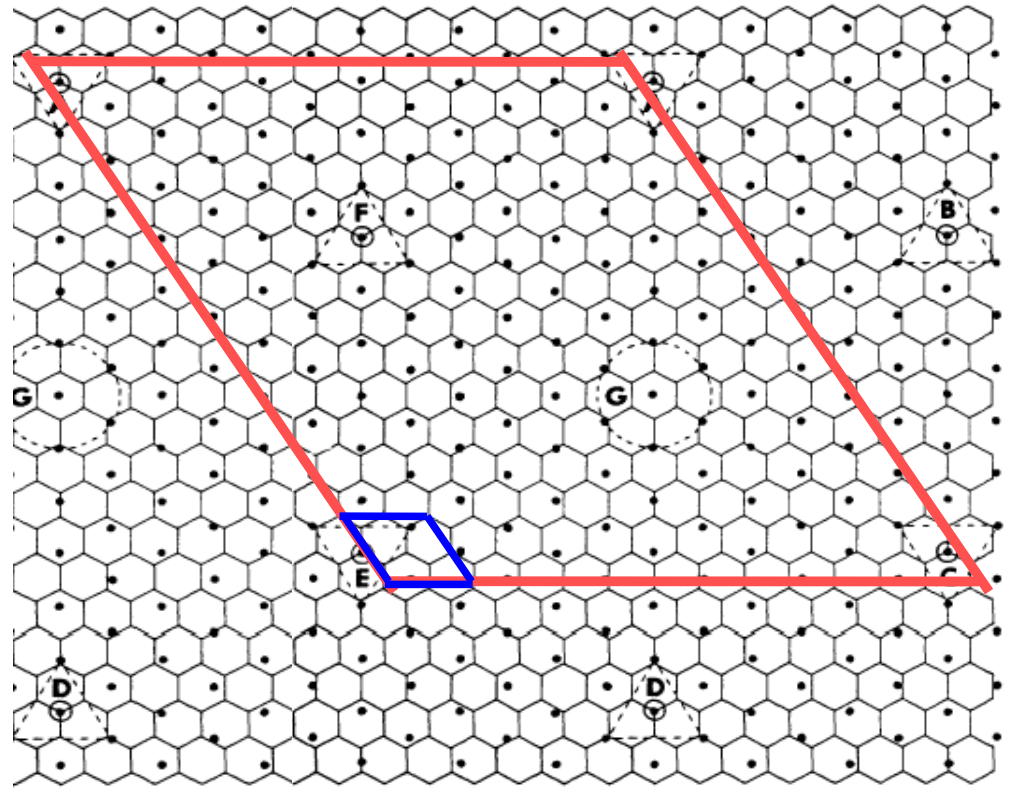


W.Chen et al Surf.Sci.596,176 (2005)
E.Rollings et al J.Phys.Chem. Sol 67, 2172 (2006)
F.Owman et al. Surf. Sci. 369, 126 (1996)
M.-H.Tsai et al. Phys. Rev. B45, 1327 (1992)
Th.Seyller et al Surf. Sci. 600, 3906 (2006)
E.K.Emtsev et al. Mater. Sci. Forum 556-557, 525 (2007)

$\sqrt{3} \times \sqrt{3}$ R30

F.Varchon et al., PRL. 99, 126805, (2007)

A.Mattausch et al. PRL99, 076802, (2007)



$6\sqrt{3} \times 6\sqrt{3}$ R30

F.Varchon et al., Phys.Rev.B 77, 235412 (2008)

S.Kim et al. Phys. Rev.Lett 100.176802 (2008)

Nanostructuring of the first C layer

Ab initio

F.Varchon et al, Phys. Rev. B (2008)

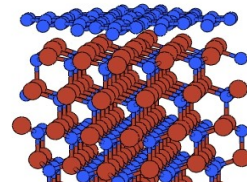
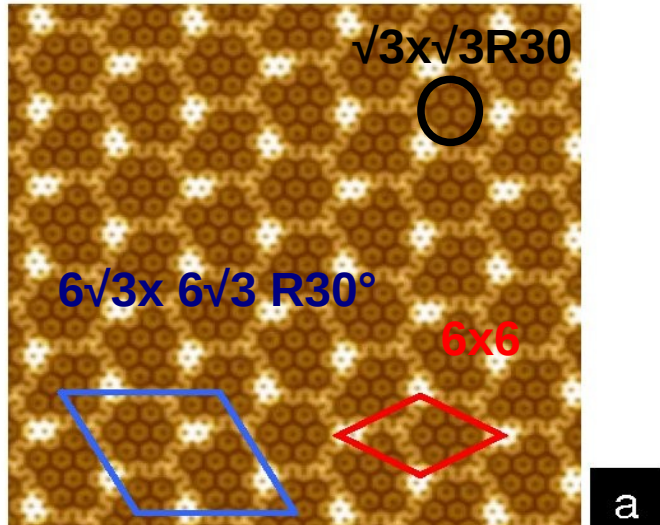
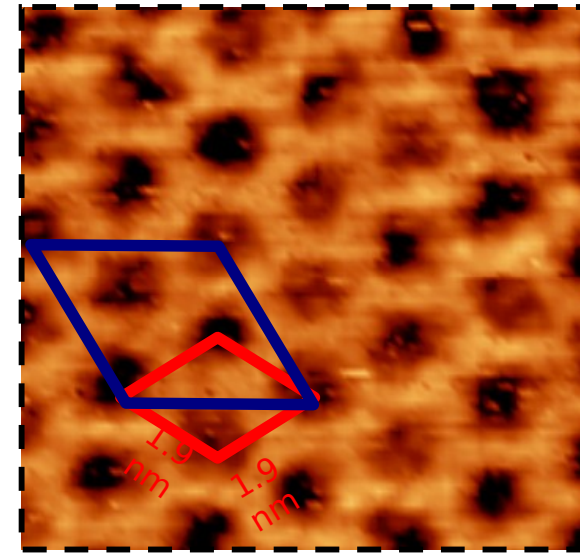


Image STM (0.2 V, 300 K)

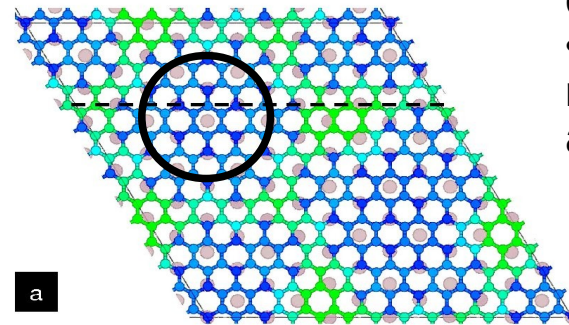
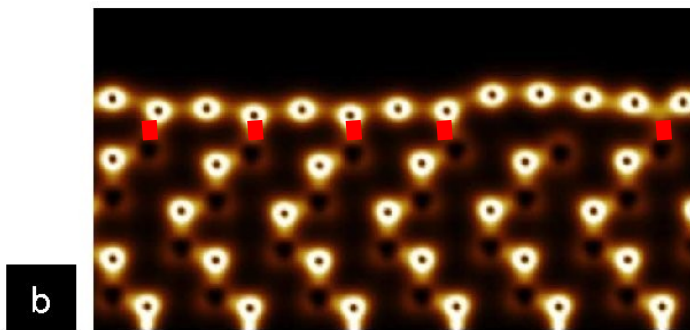
P.Mallet et al., Phys Rev B74, 041403 (R) (2007)



10 × 10 nm²

- mosaic pattern with local $\sqrt{3} \times \sqrt{3} R30^\circ$
- apparent 6X6 reconstruction
- Corrugation : 1.2 Å (STM : 1-1.5 Å)

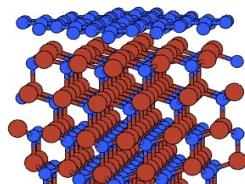
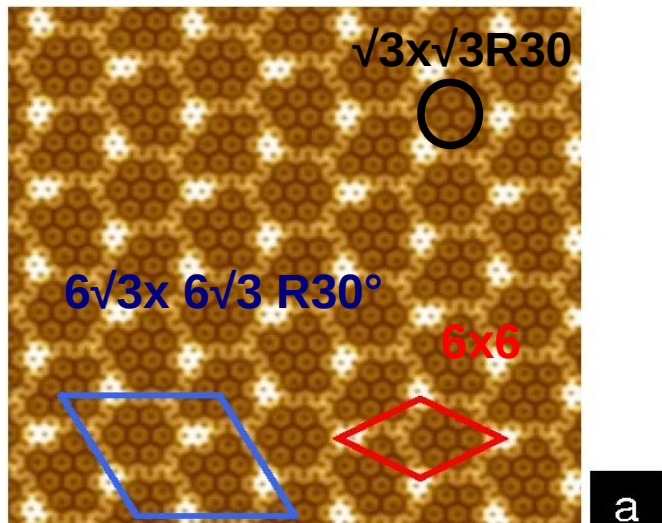
- grains : $\sqrt{3} \times \sqrt{3} R30^\circ$ matching regions covalent bond
- frontier : not in register no bond atom higher



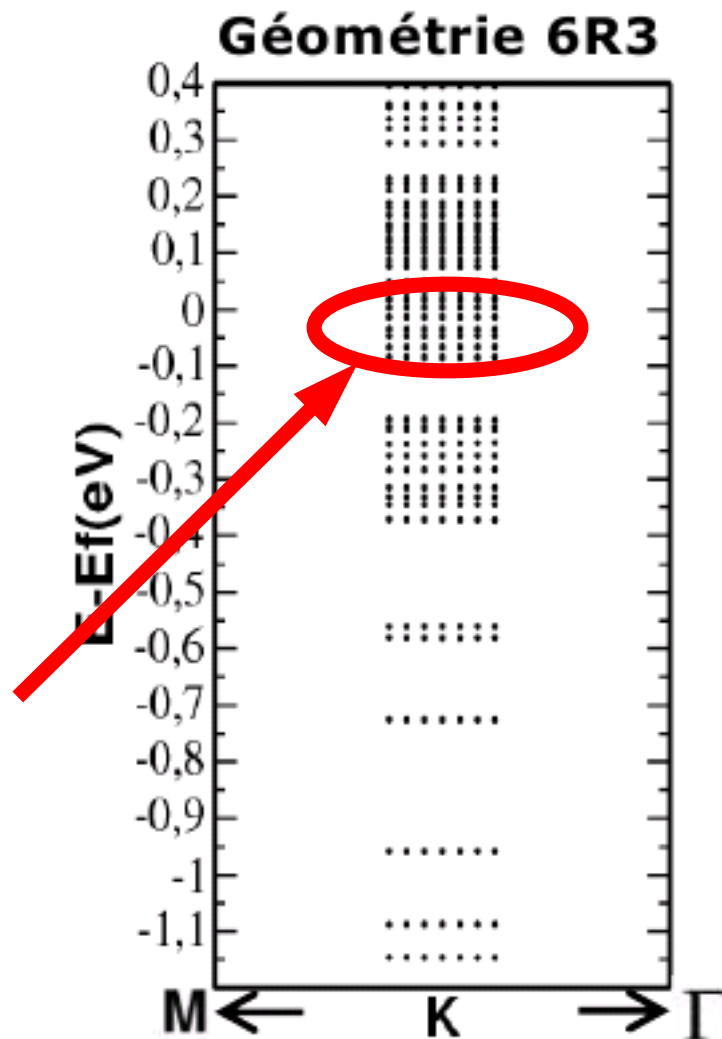
Nanostructuring of the first C layer

Ab initio

F.Varchon et al, Phys. Rev. B (2008)



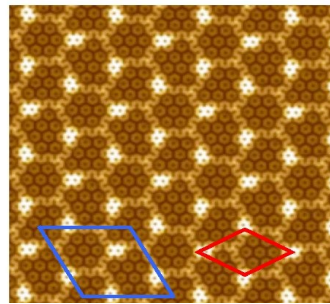
F.Varchon PhD, 2009



VASP : 1316 atomes : 13x13 graphène sur 4 biplans de SiC en $6\sqrt{3}\times 6\sqrt{3}$ R30

Un an de calcul sur une SGI 350 avec 8 processeurs (6 mois réels)

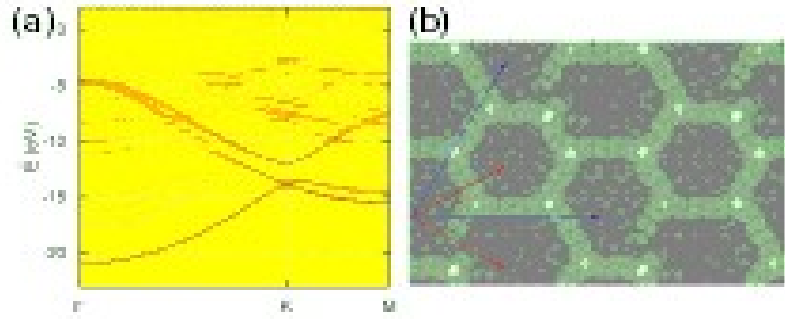
deuxième plan de C : limite SiC à 2 biplans
essais de modification des états d'interface, de diffusion, de croissance trop long



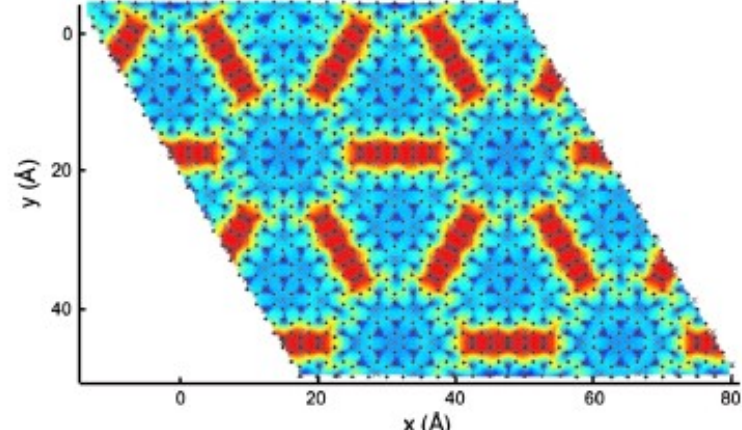
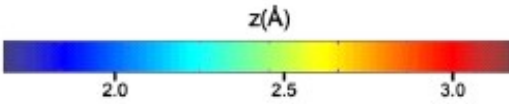
SIESTA

Origins of anomalous electronic structures of epitaxial graphene on silicon carbide

Seungeul Kim,¹ Jisoon Ihm,¹ Hyoung Joon Choi,² and Young-Woo Son^{2,1*}



EDIP



Potentiels classiques

E.Lampin et al, J.Appl. Phys. 107, 103514 (2010)

C sp² et sp³ + liaisons Si-C et C-C

G.Lucas et al JPCM 22, 035802 (2010)

E.Lampin, C.Priester, C.Krzeminski, LM J.Appl. Phys. 107, 103514 (2010)

M.Z.Bazant, E.Kaxiras, PRL 77, 4370 (1996) pour Si

G.Lucas, M.Bertolus, L.Pizagalli JPCM 22, 035802 (2010) adaptation pour SiC

$$E = \sum_i E_i,$$

$$E_i = \sum_{j \neq i} V_2(\vec{r}_i, \vec{r}_j, Z_i) + \sum_{j \neq i} \sum_{k \neq i, k > i} V_3(\vec{r}_i, \vec{r}_j, \vec{r}_k, Z_i).$$

$$Z_i = \sum_{m \neq i} f(r_{im}) \quad f(r) = \begin{cases} 1, & r < c \\ \exp \left[\alpha / \left(1 - \left(\frac{a-c}{r-c} \right)^3 \right) \right] \Delta(r), & c < r < a \\ 0, & r > a. \end{cases}$$

$$V_2(r_{ij}, Z_i) = A \left[\left(\frac{B}{r_{ij}} \right)^\rho - p(Z_i) \right] \exp \left(\frac{\sigma}{r_{ij} - a} \right)$$

$$p(Z) = \exp(-\beta Z^2)$$

$$V_3(\vec{r}_{ij}, \vec{r}_{ik}, Z_i) = g(r_{ij})g(r_{ik})h(l_{ijk}, Z_i)$$

$$l_{ijk} = \cos \theta_{ijk} = \vec{r}_{ij} \cdot \vec{r}_{ik} / r_{ij} r_{ik}$$

$$g(r) = \exp \left(\frac{\gamma}{r - a} \right) \quad \text{Stillinger-Weber}$$

$$h(l, Z) = \lambda[(1 - \exp(-Q(Z)(l + \tau(Z))^2)) + \eta Q(Z)(l + \tau(Z))^2],$$

$\tau(Z)$ angle d'équilibre

$$\tau(Z) = l_0(Z) = -\cos \theta_0(Z)$$

$$\omega(Z)^{-2} = Q(Z) = Q_0 \exp(-\mu Z)$$

$\omega(Z)$ force de l'interaction

$$\tau(Z) = u_1 + u_2(u_3 \exp(-u_4 Z) - \exp(-2u_4 Z))$$

13 paramètres pour Si

SiC

A : garde Si optimise C
Si-C moyenne
+ correction

$$\Delta(r) = \begin{cases} 1, & r < c \\ \exp\left(\frac{\alpha}{1-x^{-3}}\right), & c < r < a - \delta \\ 0, & r > a - \delta, \end{cases}$$

B: tout réoptimisé

$$\delta = 0.3 \text{ \AA}$$

$$f(r) = \begin{cases} 1, & r < c \\ \exp\left[\alpha / \left(1 - \left(\frac{a-c}{r-c}\right)^3\right)\right] \Delta(r) & c < r < a \\ 0, & r > a. \end{cases}$$

$$V_2(r_{ij}, Z_i) = A \left[\left(\frac{B}{r_{ij}}\right)^\rho - p(Z_i) \right] \exp\left(\frac{\sigma}{r_{ij} - a}\right) \Delta(r_{ij})$$

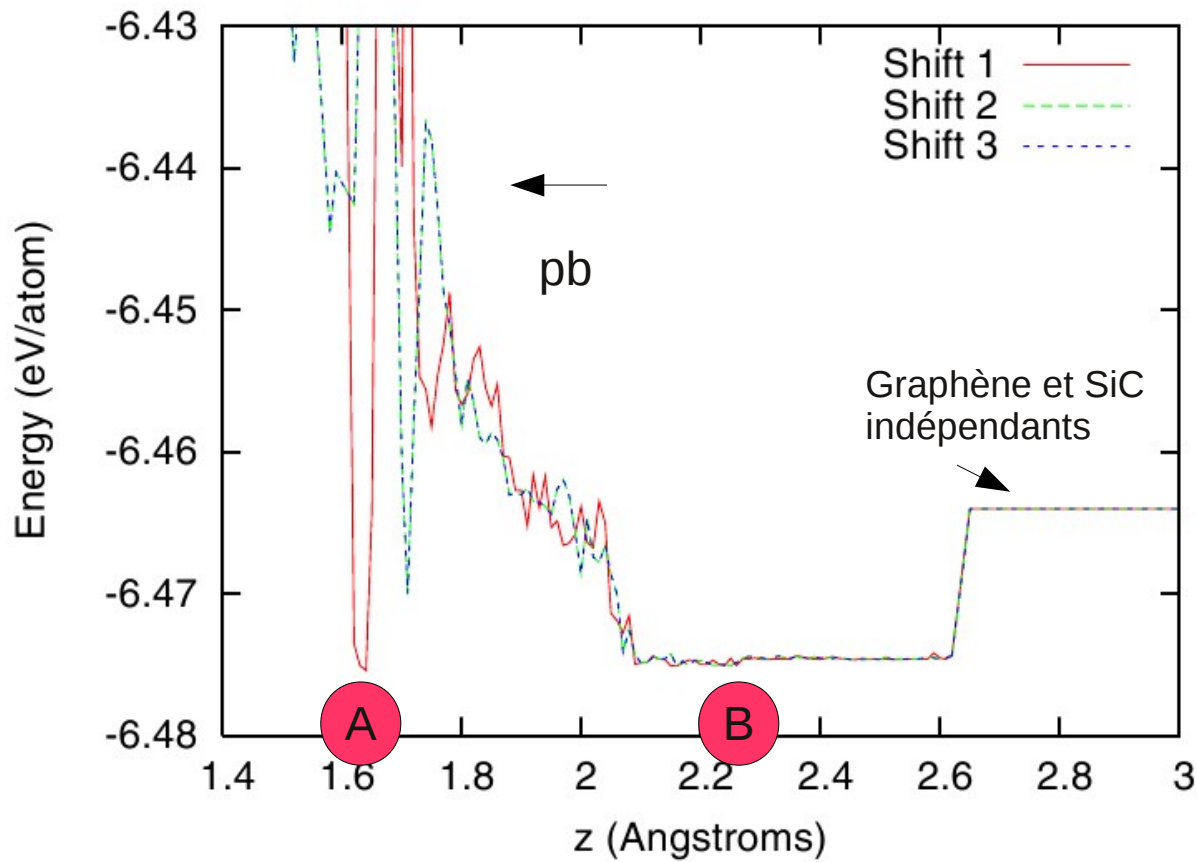
$$V_3(\vec{r}_{ij}, \vec{r}_{ik}, Z_i) = g(r_{ij})g(r_{ik})h(l_{ijk}, Z_i) \Delta(r_{ij}) \Delta(r_{ik})$$

13X13 graphène sur $6\sqrt{3}\times 6\sqrt{3}$ R30 SiC (6 biplans)

biplan du bas gelé
gradients conjugués

Fait varier la distance initiale plan de graphène – SiC de 1.5 à 3 Å par pas de 0.01 Å

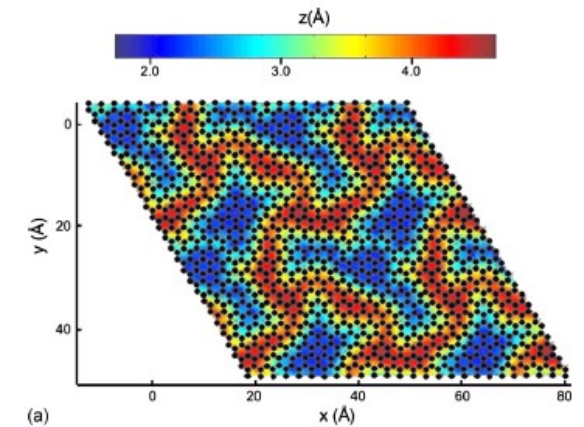
- 1 : C au dessus Si
- 2 : centre hexagone au dessus Si
- 3 : milieu C-C graphène au dessus Si



2 et 3 même résultat

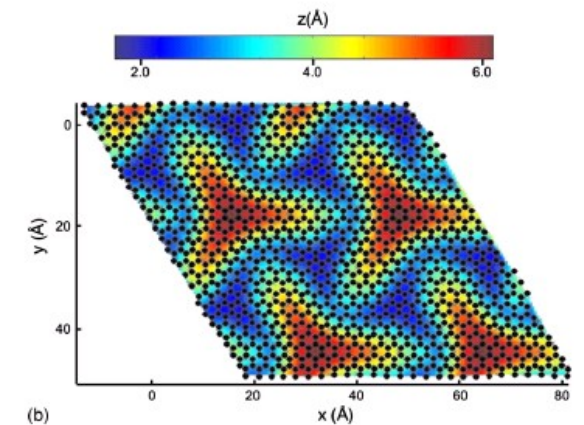
A

1.63



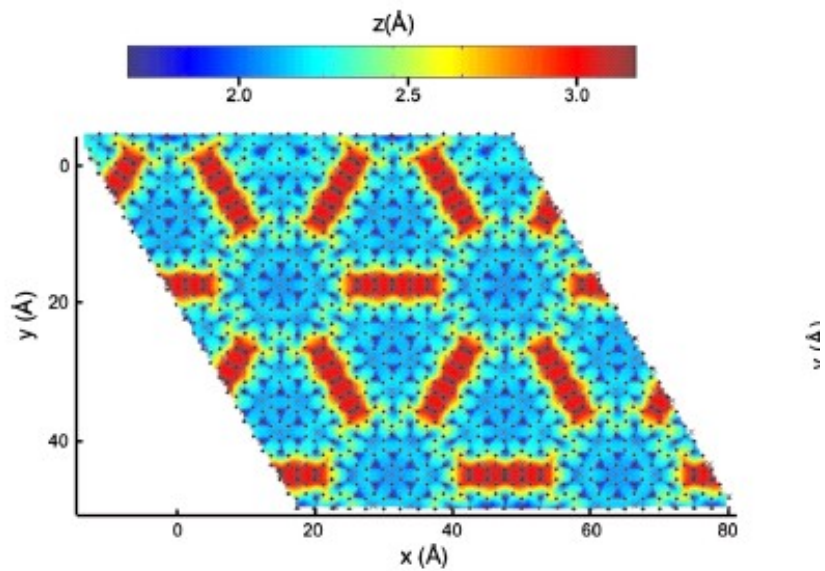
B

2.26

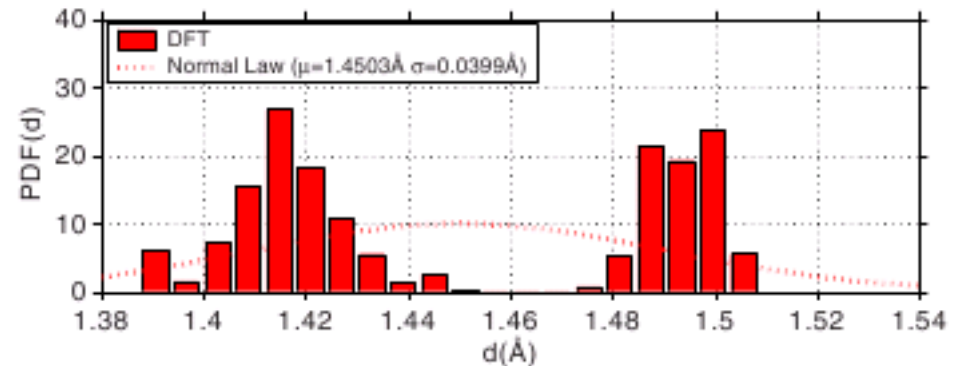
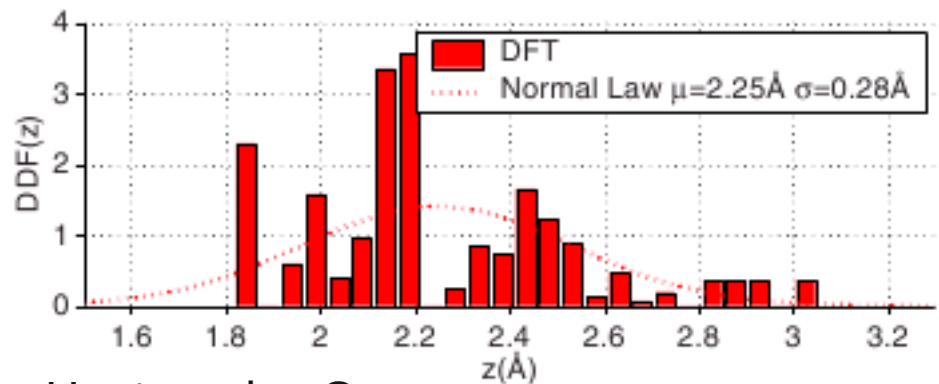
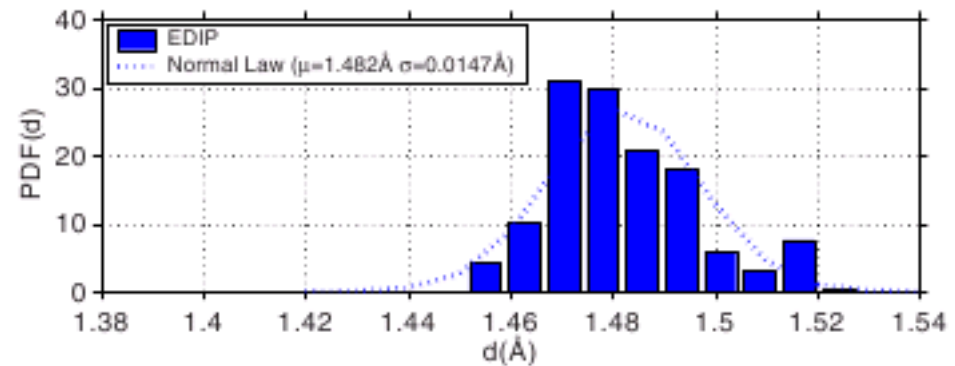
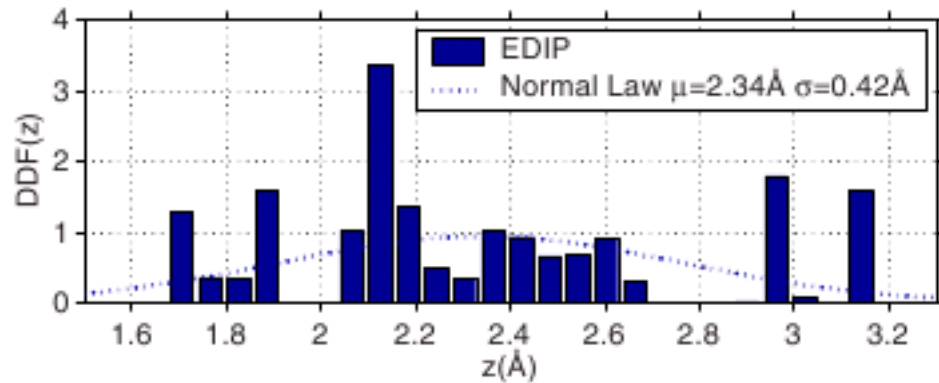
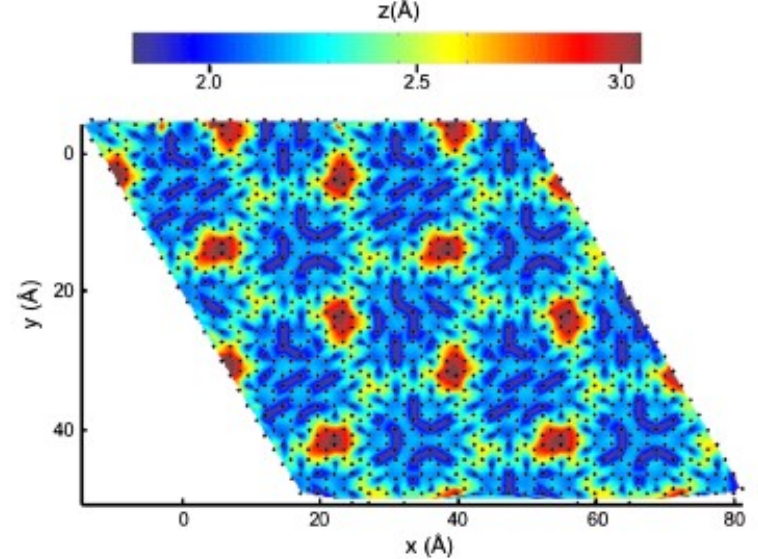


Pré-relaxation du graphène : descend les C qui sont proches voisins de Si

EDIP



Ab initio



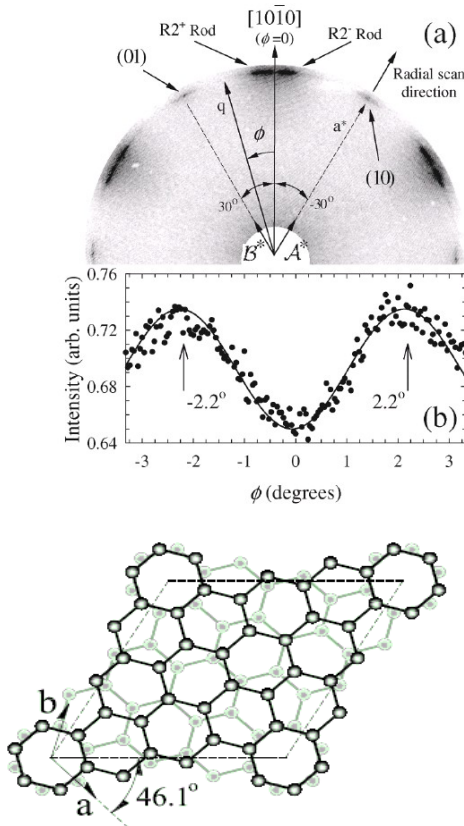
Hauteur des C

Distance C-C dans le plan

2. C Face : Rotated bilayers

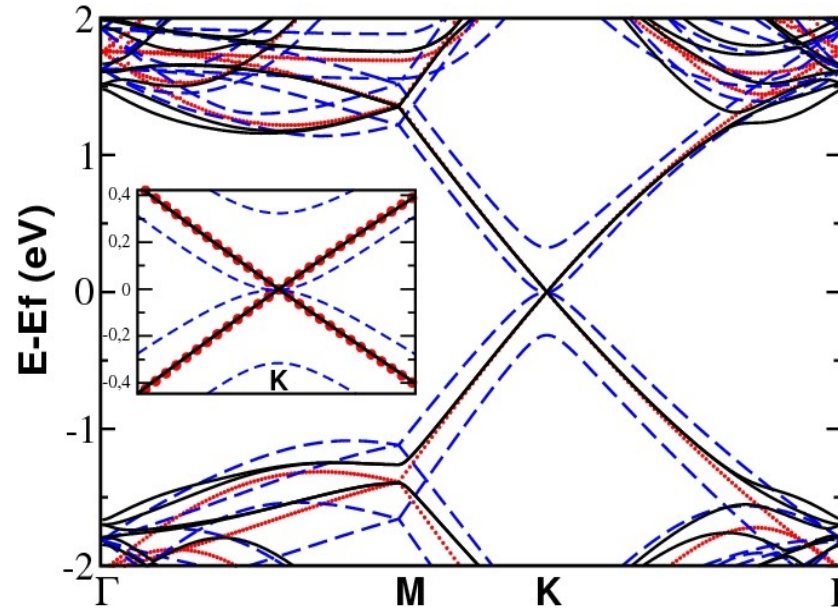
Van Bommel 1975

Weak interaction : no long range order for growth
no Bernal stacking (**twisted layers**)



$\sqrt{13} \times \sqrt{13} R \pm 46.1^\circ$
commensurate with SiC

--- AB bilayer
 Monolayer
 — Twisted bilayer



Twist preserves linear dispersion

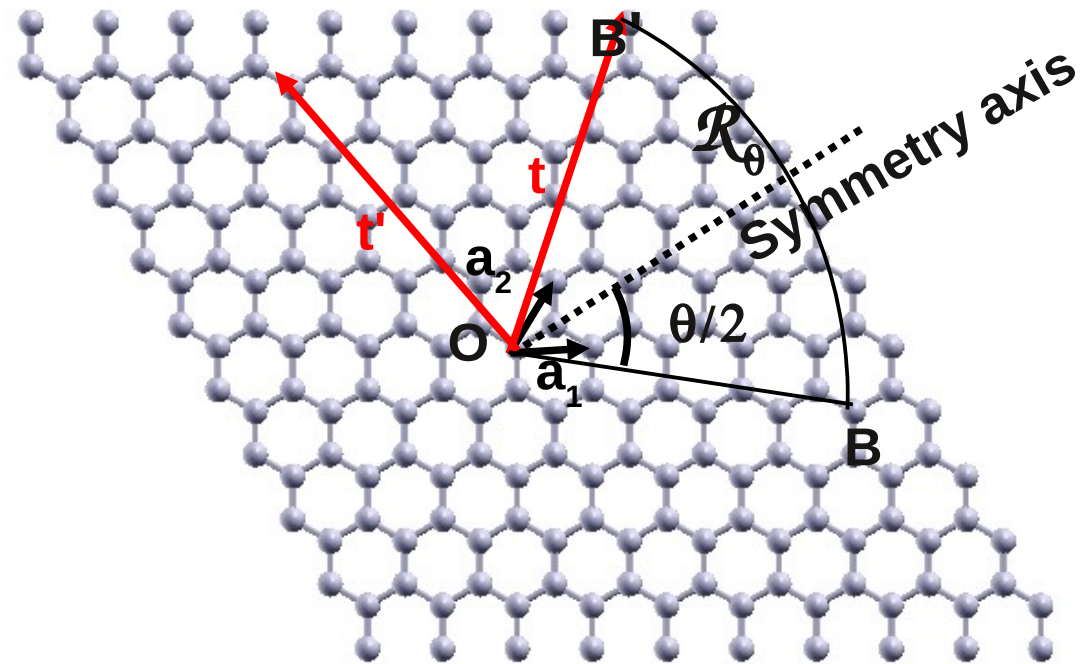
J. Hass et al., PRL 100, 125504 (2008)

2. Rotated bilayers: renormalisation of the velocity

L.Magaud, D.Mayou, G.Trambly de Laissardière

Ab initio (VASP) => periodic system

Common cell for two layers rotated by θ



Common cell defined by:

$$\mathbf{t} = n\mathbf{a}_1 + m\mathbf{a}_2$$

$$\mathbf{t}' = m\mathbf{a}_1 + (n+m)\mathbf{a}_2$$

Rotation angle:

$$\cos(\theta) = 2 \cos^2(\theta/2) - 1 = \frac{n^2 + 4nm + m^2}{2(n^2 + nm + m^2)}$$

ab initio calculation + TB fit: small angles/ shift / asymmetric bilayer

Small angles $(6,7) \theta=5.08^\circ$

TB scheme

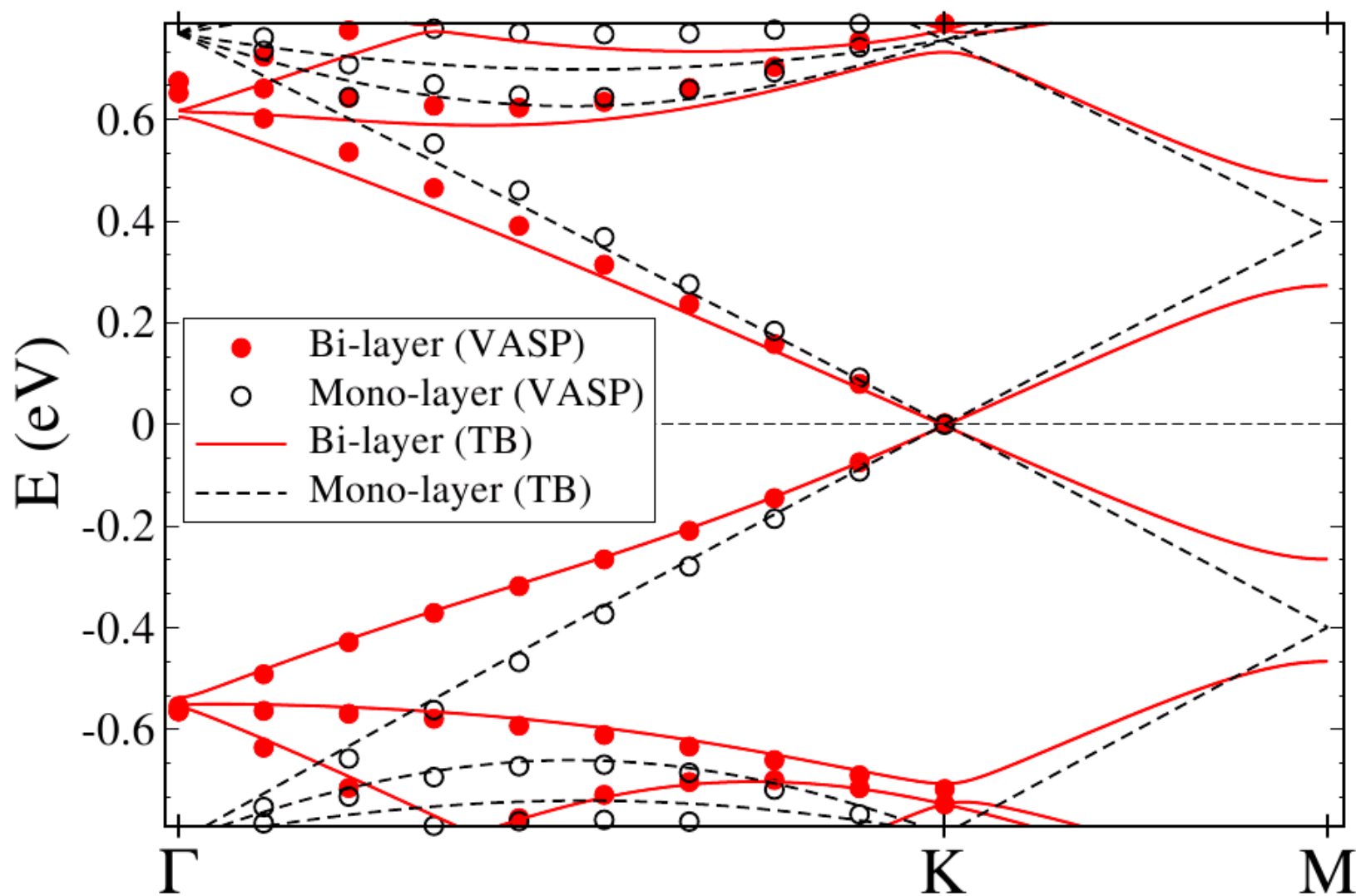
$$V_{pp\pi} = -\gamma_0 \exp\left(q_\pi \left(1 - \frac{d}{a}\right)\right)$$

$$\gamma_0 = 2.7 \text{ eV}, \gamma_1 = 0.48 \text{ eV}$$

$$a = 1.42 \text{ \AA}, a_1 = 3.35 \text{ \AA}$$

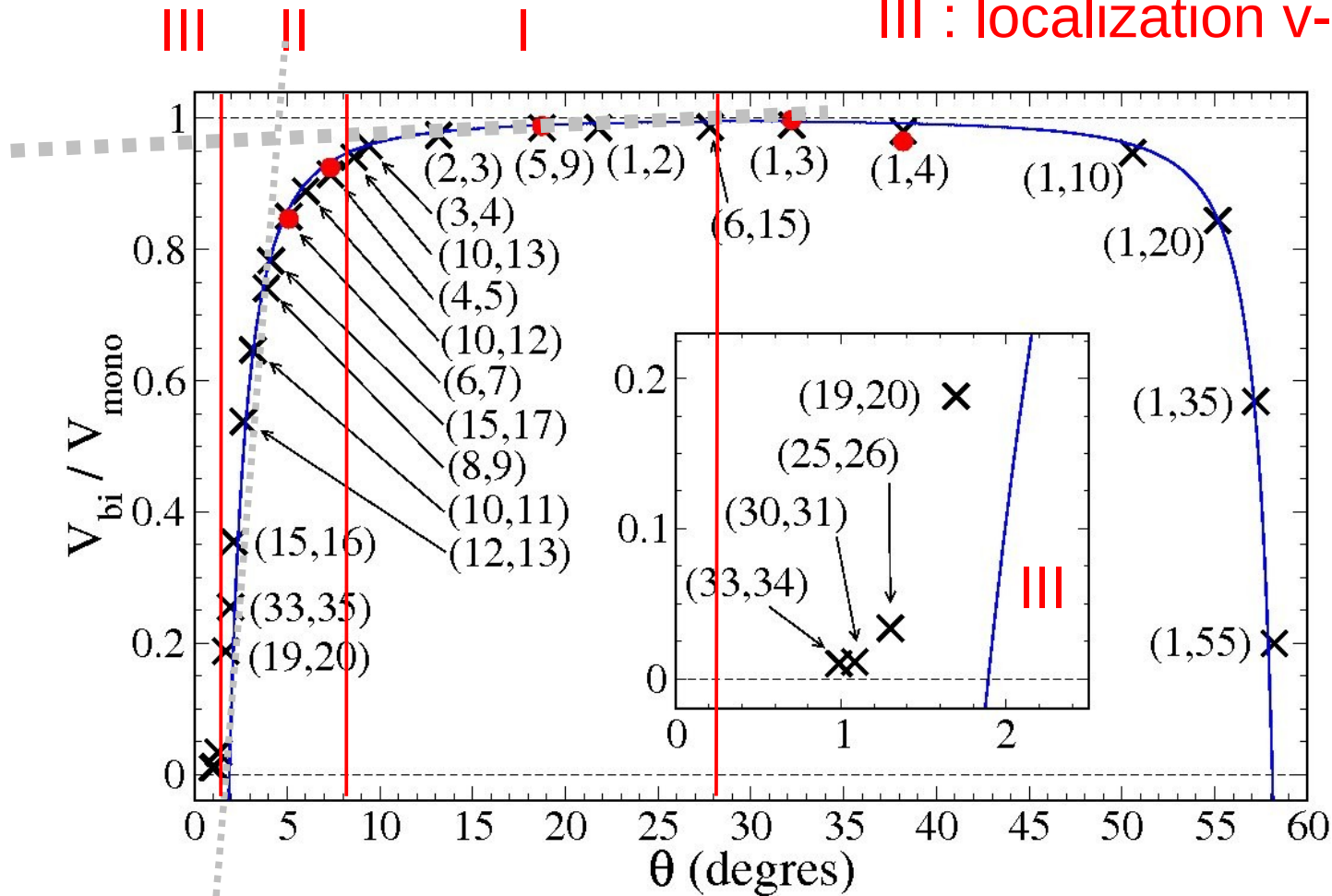
$$V_{pp\sigma} = \gamma_1 \exp\left(q_\sigma \left(1 - \frac{d}{a_1}\right)\right) \text{ with } \frac{q_\sigma}{a_1} = \frac{q_\pi}{a}$$

fitted on AA, AB, (1,3) et (1,4)

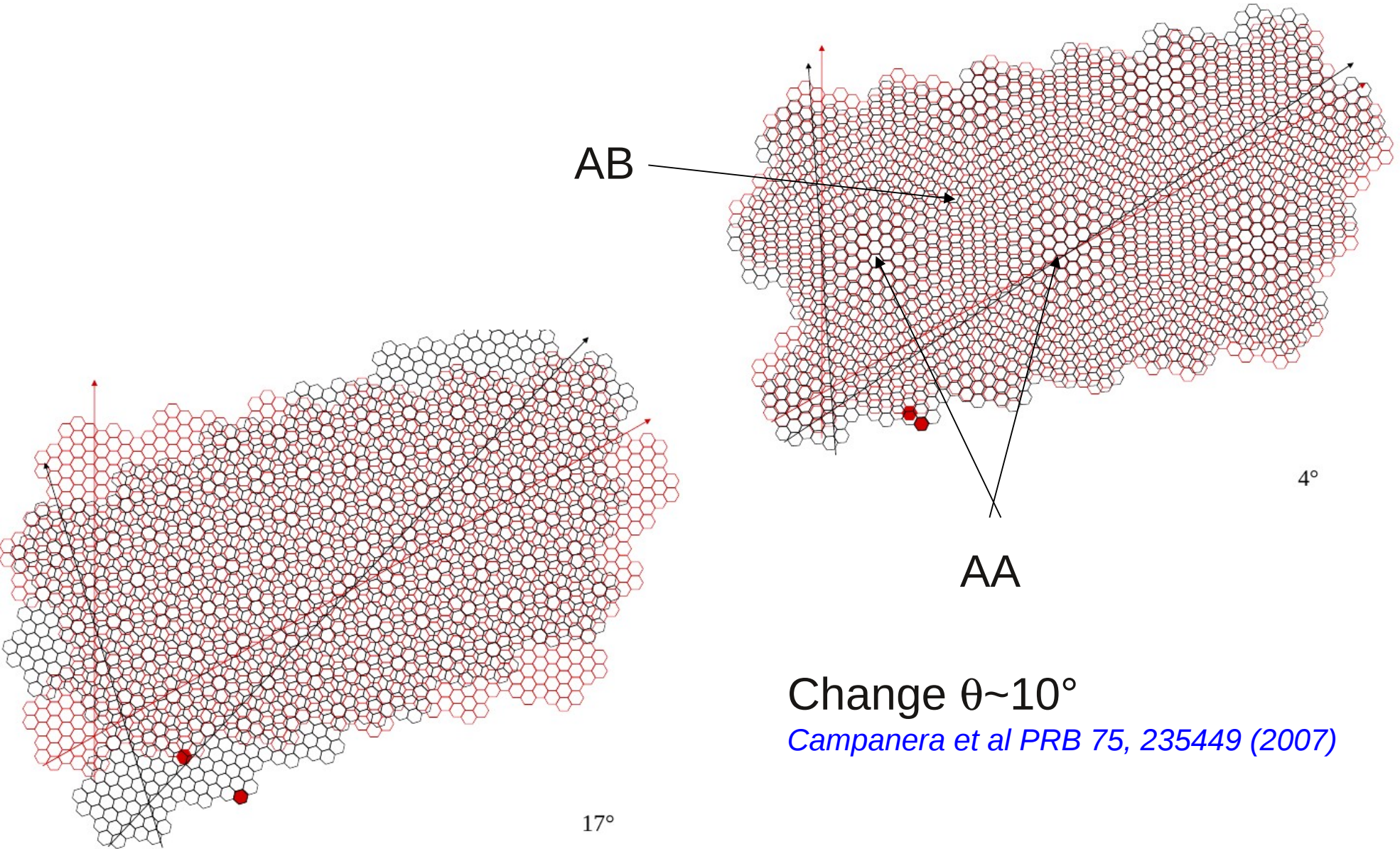


3. Rotated bilayers: renormalisation of the velocity

I : decoupling
 II : Renormalisation of velocity
 III : localization $v \rightarrow 0$



3. Rotated bilayers: renormalisation of the velocity



First regime :

- two decoupled graphene layers
- no change of velocity

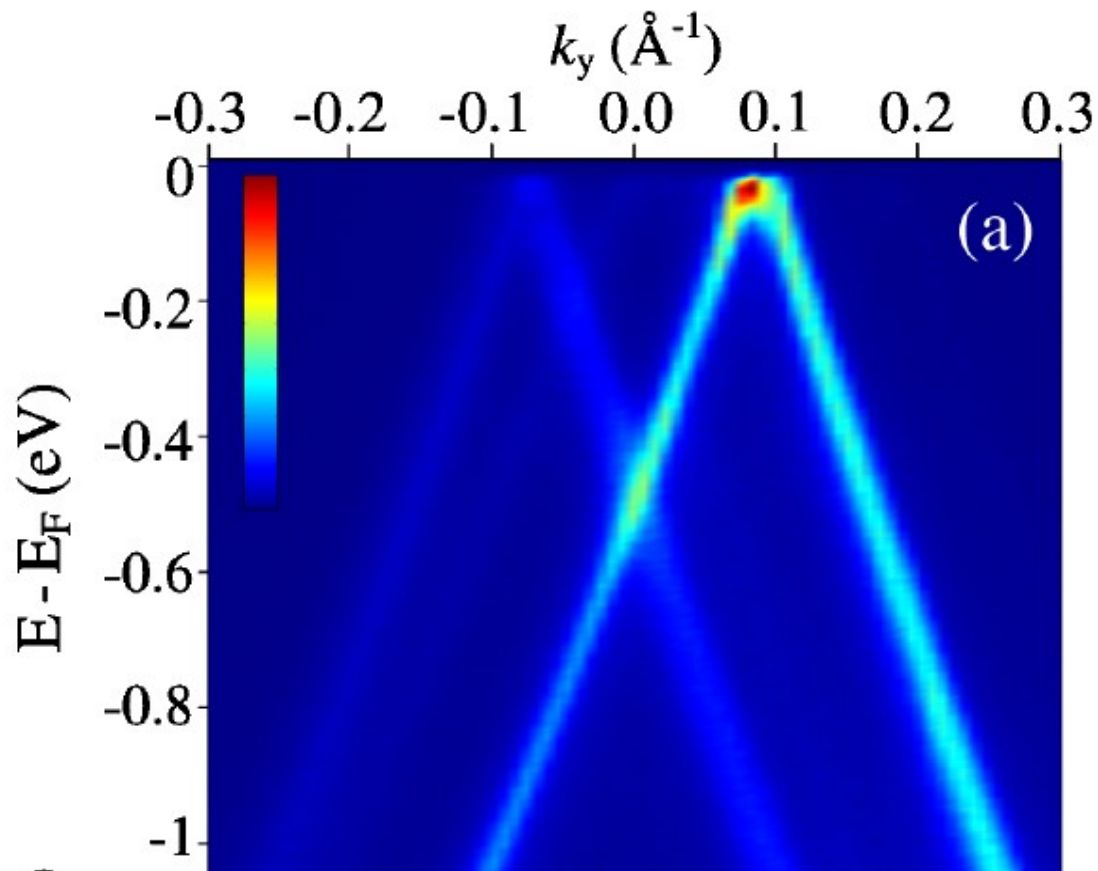
PRL 103, 226803 (2009)

PHYSICAL REVIEW LETTERS

week ending
27 NOVEMBER 2009

First Direct Observation of a Nearly Ideal Graphene Band Structure

M. Sprinkle,¹ D. Siegel,² Y. Hu,¹ J. Hicks,¹ A. Tejada,^{3,4} A. Taleb-Ibrahimi,⁵ P. Le Fèvre,⁴ F. Bertran,⁴ S. Vizzini,^{6,7} zara,² and E. H. Conrad¹

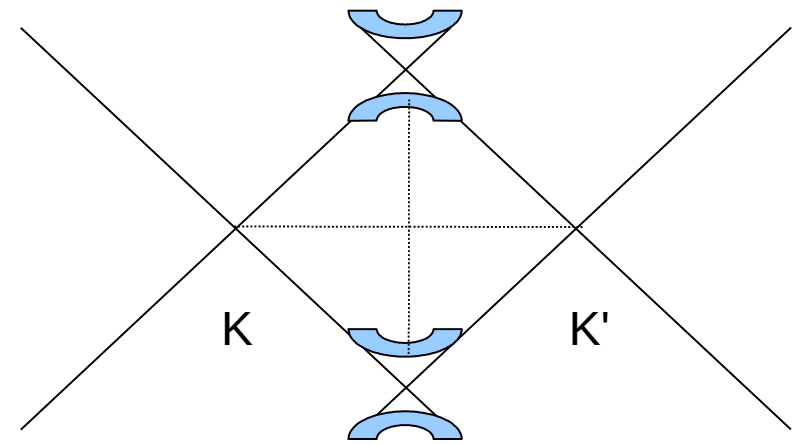


11 layers

Multilayer graphene=
isolated graphene sheets

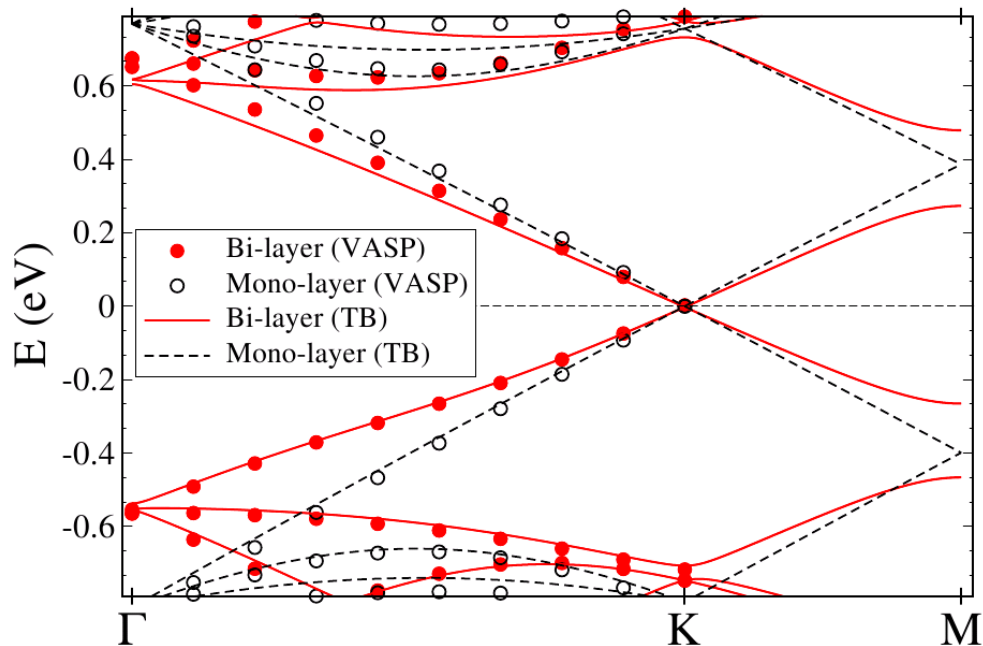
Second and third regime :

- Renormalization of velocity
- Two coupled graphene layers



Single Layer Behavior and Its Breakdown in Twisted Graphene Layers

A. Luican¹, Guohong Li¹, A. Reina², J. Kong³, R. R. Nair⁴, K. S. Novoselov⁴, A. K. Geim^{4,5}, E.Y. Andrei¹



Twisted layers from growth on Ni
STS LL

$\theta > 20^\circ$ decoupling

$3 < \theta < 20^\circ$ renormalisation of velocity

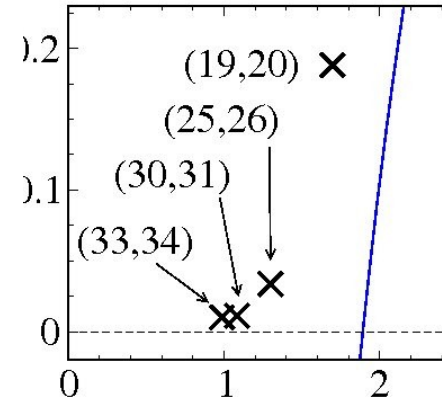
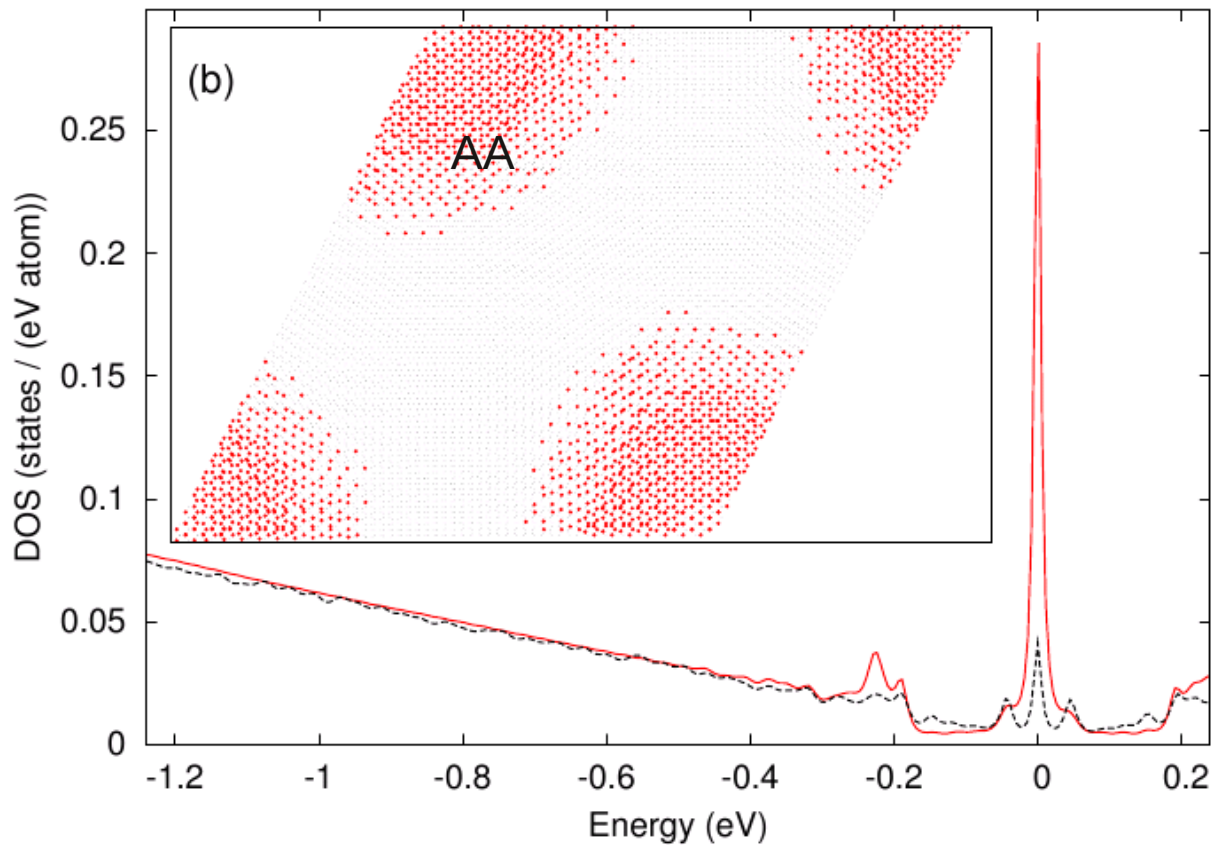
$\theta < 3^\circ$ van Hove singularity and localisation

third regime :

- Localization $\nu \rightarrow 0$

(30,31) (1.08°)

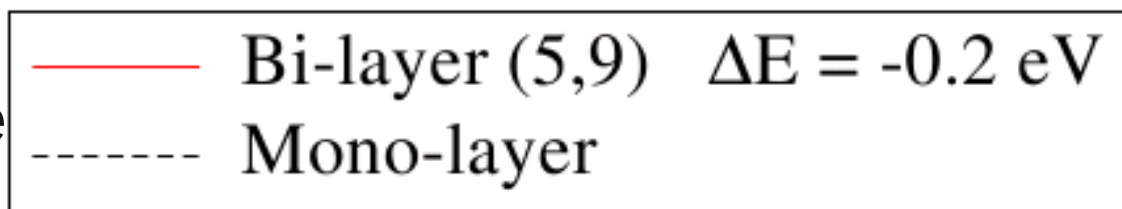
Energy (eV)



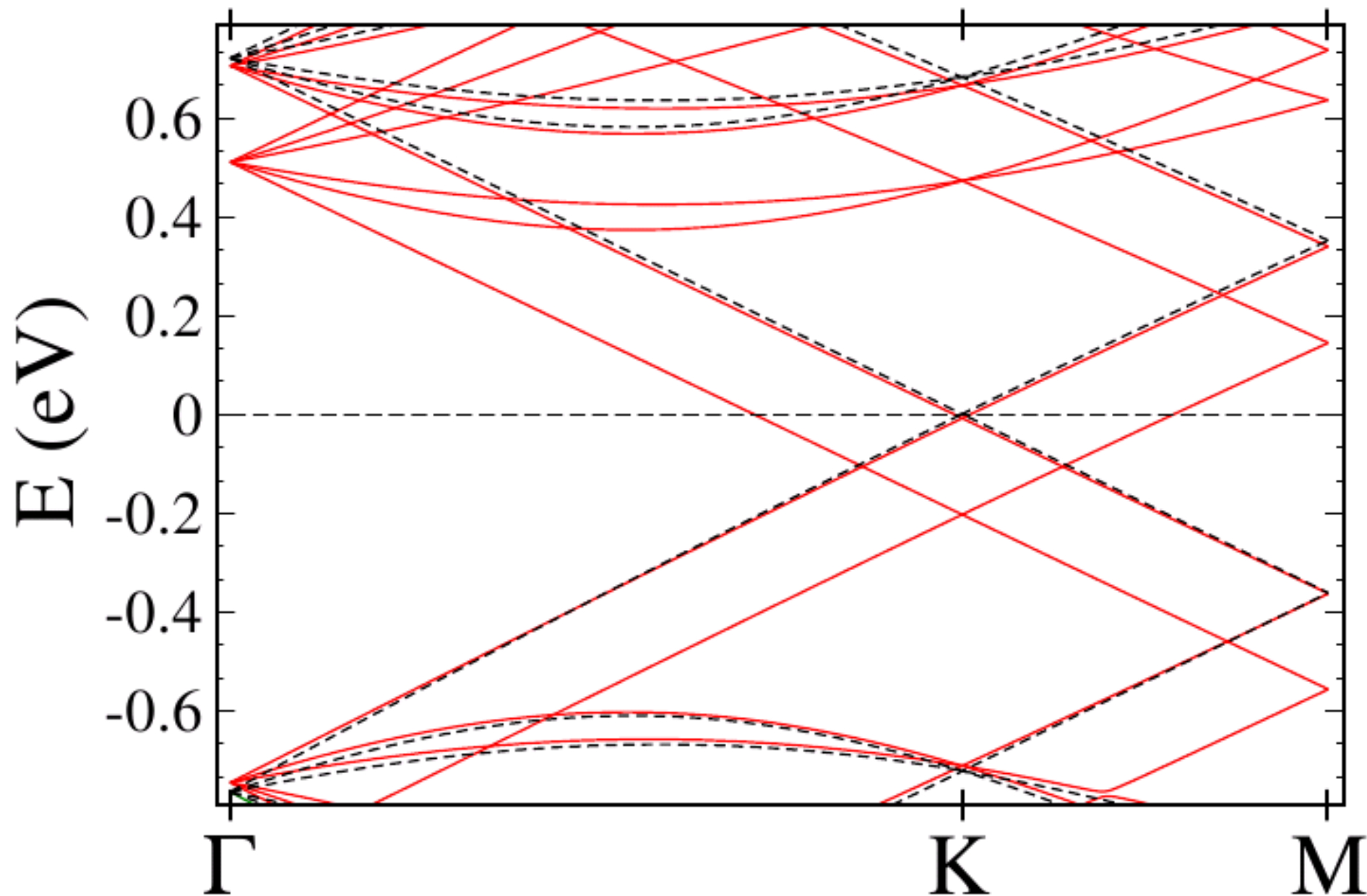
Peak at Dirac point

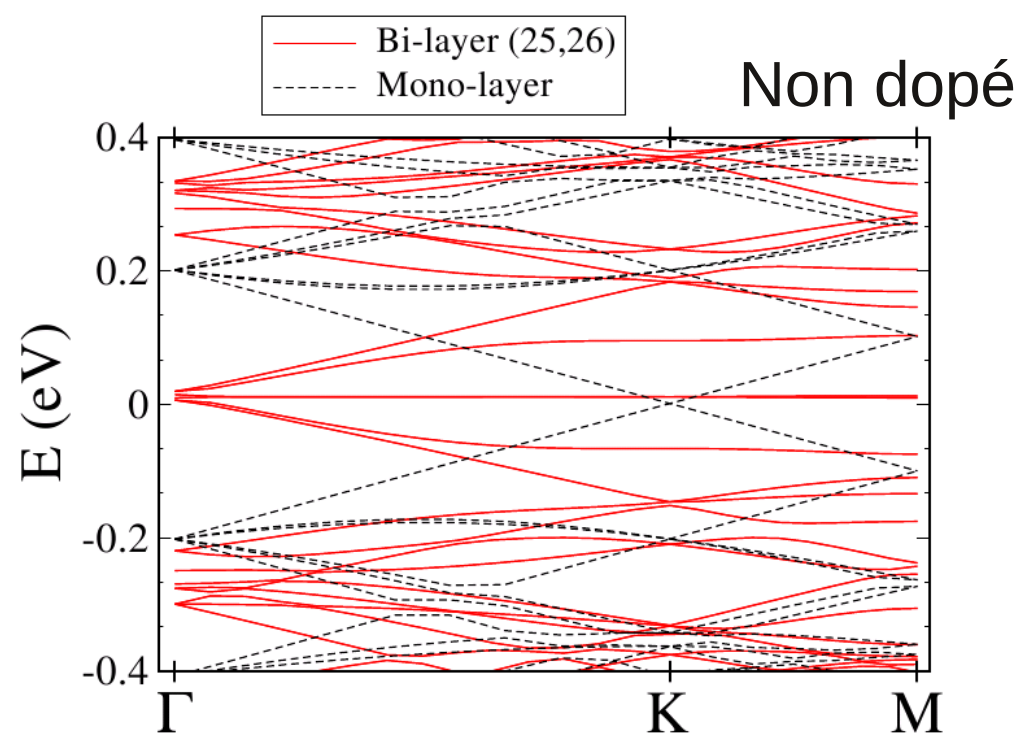
G.Trambly, D.Mayou, L.Magaud,
ArXiv : 0904.1233
NanoLetters 10, 804 (2010)

Effet du dopage
biplan asymétrique
5,9 plans découplés

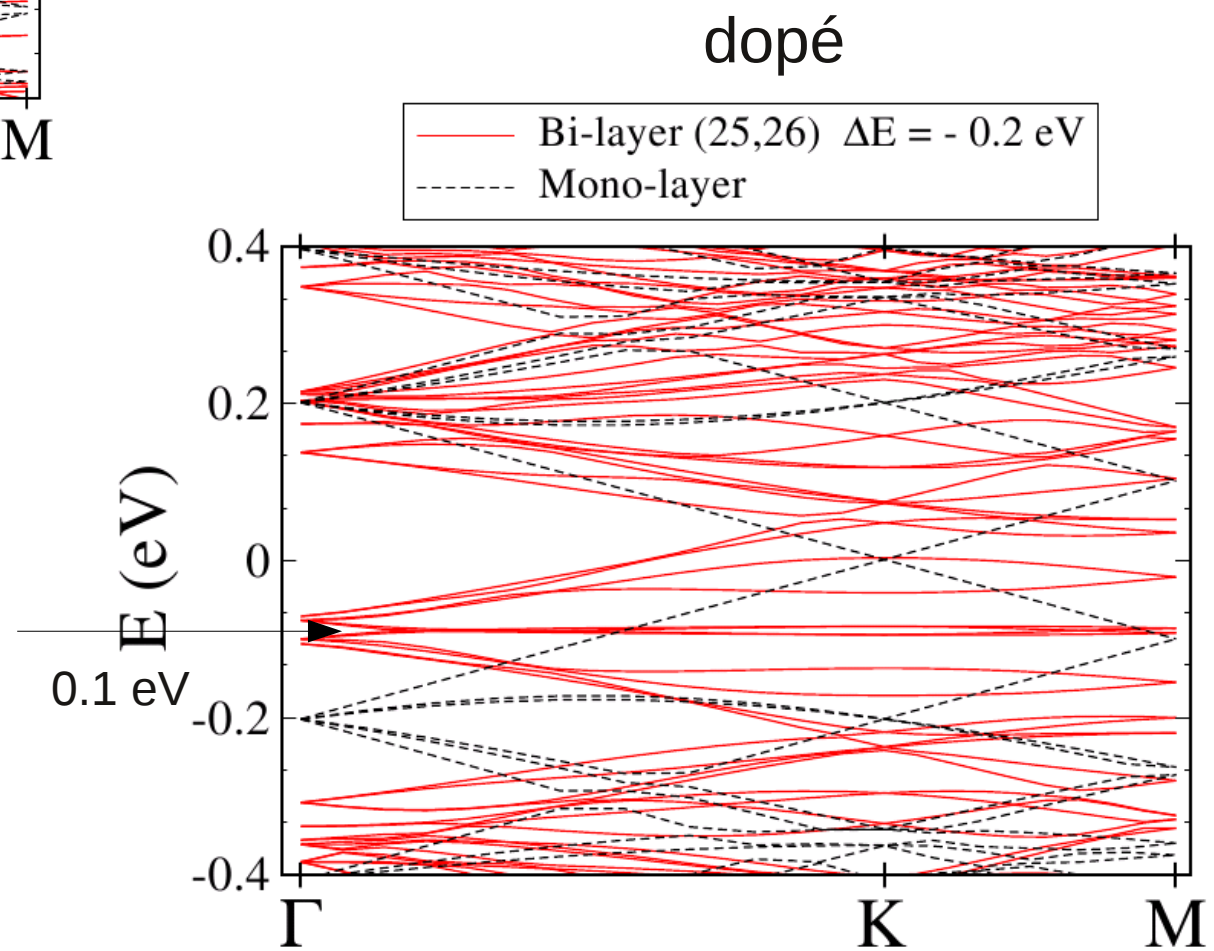
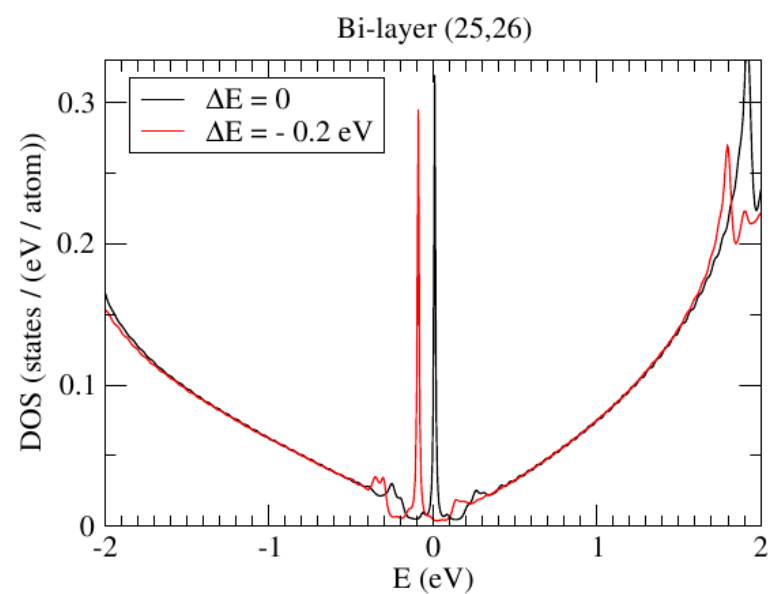


$\theta = 18.73^\circ$





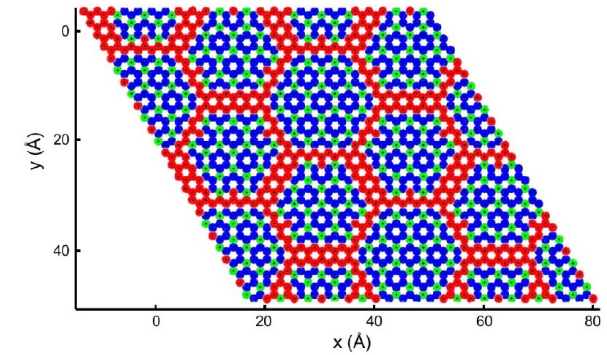
(25,26) $\theta=1.26^\circ$



Conclusion

➤ Si - face

- strong coupling
- 1st layer = bufferlayer

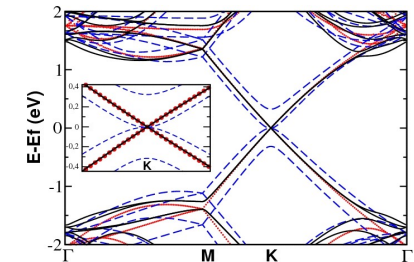
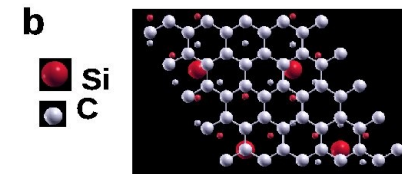


EDIP

E.Lampin et al, J.Appl. Phys. 107, 103514 (2010)

➤ C - face

- weak coupling : passivation by surface reconstruction
- graphene = 1st C layer
- no epitaxy : rotated grains
- twist : from decoupling to localization





STM **P.Mallet, J-Y.Veuillen, F.Hiebel, F.Varchon**

Theory **LM, F.Varchon, D.Mayou, F.Hiebel,
G.Trambly de Laissardière (Cergy-Pontoise)
Driss Mouhamadou, Quentin Stainer**

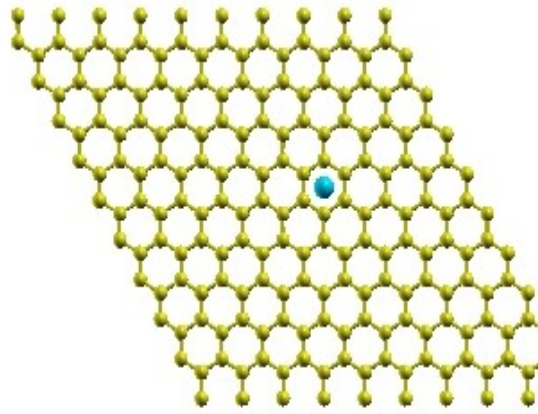
Fundings : ANR Blanche GRAPHIC
 ANR P3N NANOSIM_GRAPHENE
 Region : CIBLE 2007 and CIBLE 2008, Cluster recherche
 Nanoscience Fondation grenoble : DISPOGRAPH



Growth

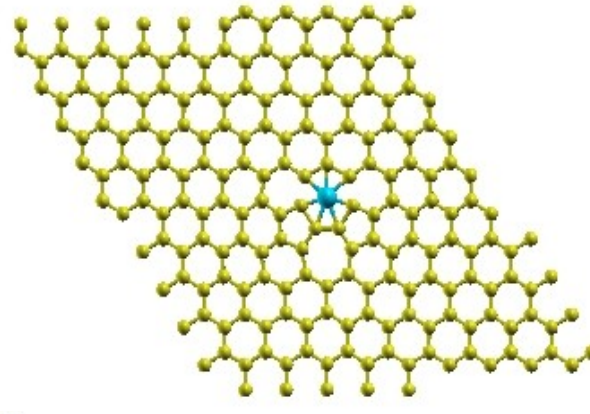
N. Camara et al, Appl. Phys. Lett. 93, 263102 (2008)

Perfect graphene



15 eV

Stone Wales defect



9 eV

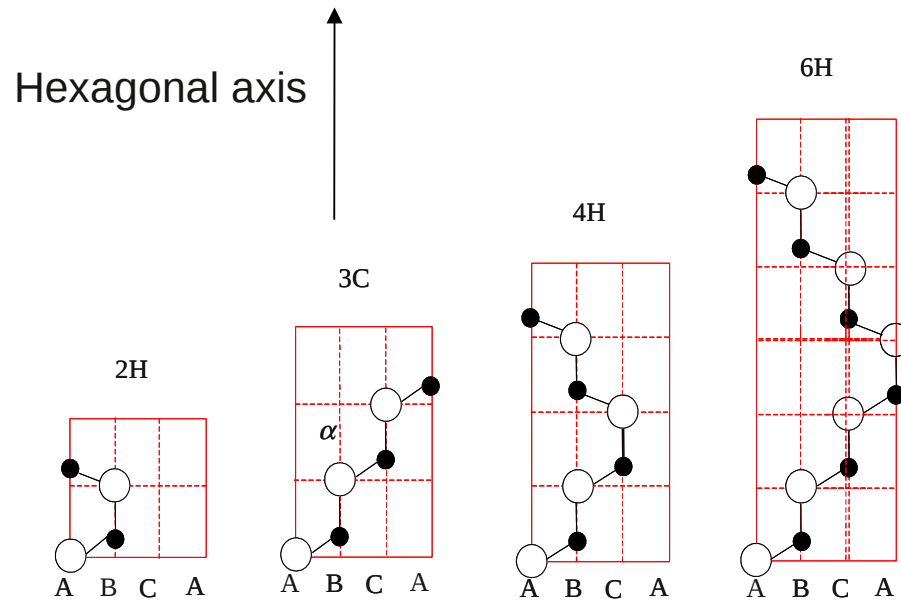
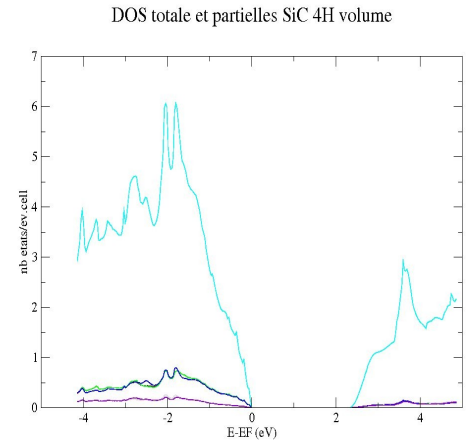
The substrate SiC

SiC : large band gap semiconductor

Si – C bilayers similar to C bilayers or Si bilayers along the (111) axis in diamond structure

Polytypes :

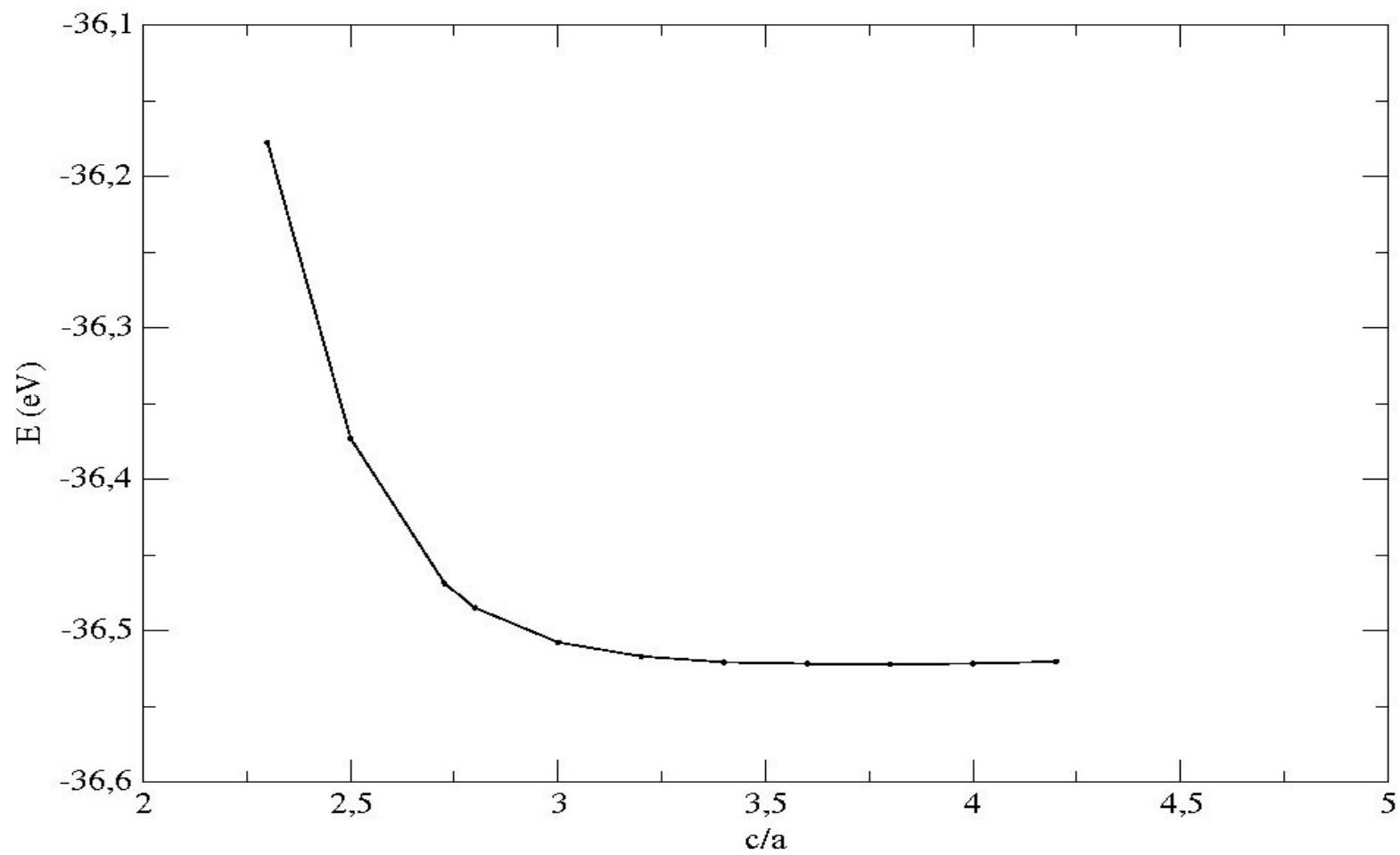
how Si-C bilayers are stacked along the hexagonal axis.
Structures very close in E

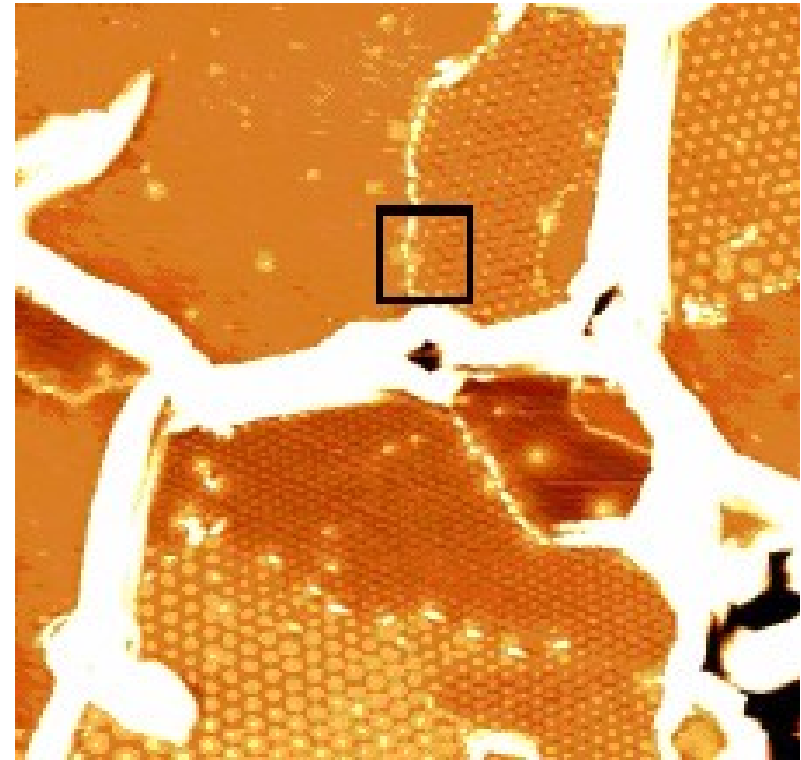
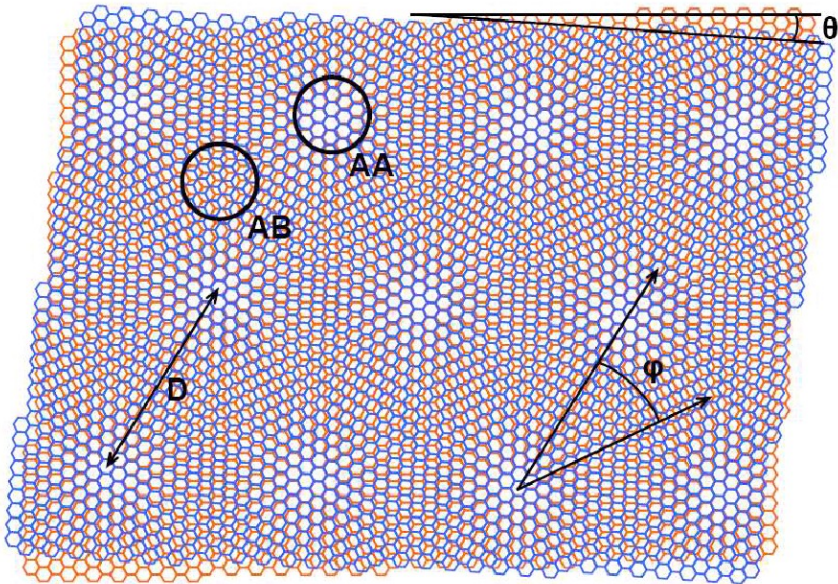


C terminated surface

Si terminated surface

graphite $E=f(c/a)$





θ : rotation angle between two graphene layers

a lattice parameter

- period of the superlattice (moiré)

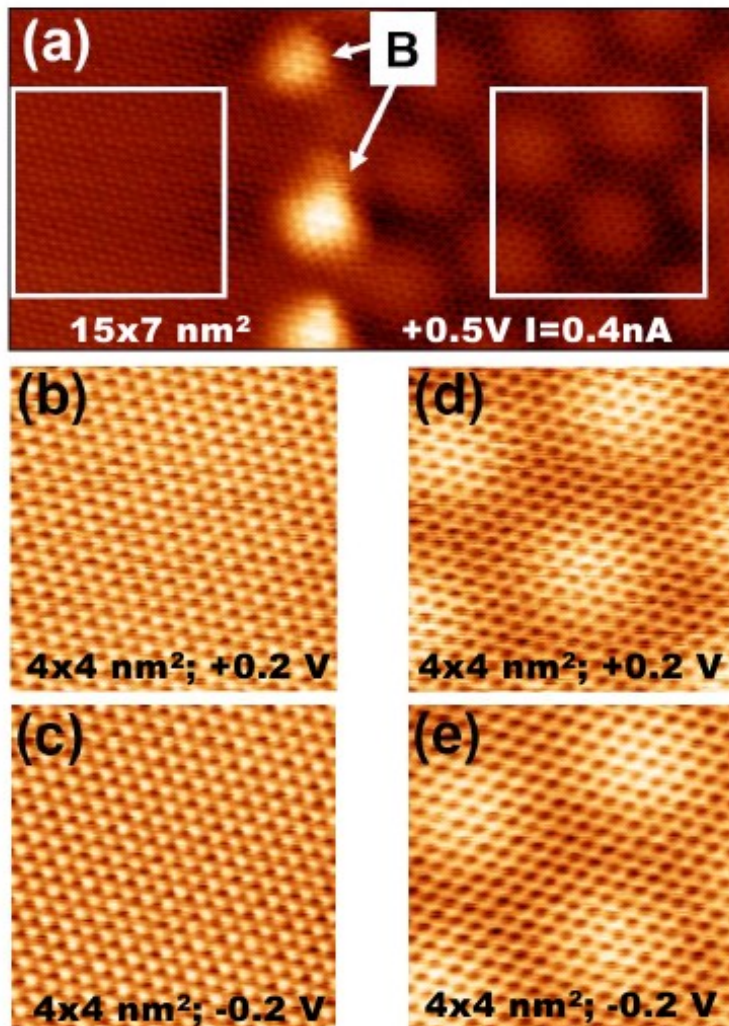
$$D = a/(2\sin(\theta/2))$$

- Angle φ between the moiré superlattice and graphene

$$\varphi = 30^\circ - (\theta/2)$$

F.Varchon et al, PRB 77, 235412 (2008)

Impact on atomic contrast



F.Varchon *et al.*, PRB 77, 165415 (2008)

We observe, in a range of small biases (below and above E_F):

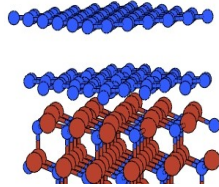
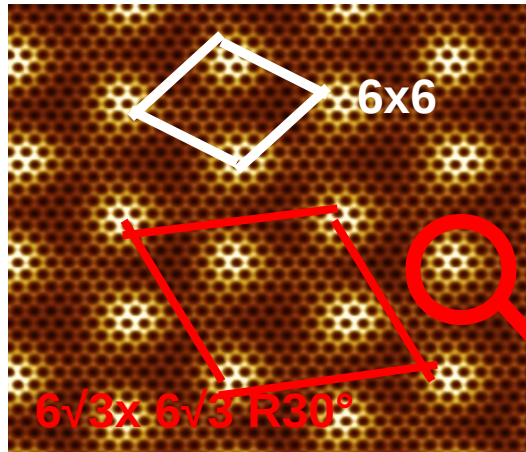
- honeycomb pattern (or a significantly reduced A/B site asymmetry) on the Moire superstructure
- triangular pattern on the flat region (bernal stacking)

Valuable indication that a single layer-like behavior can be found on rotated graphene layers.

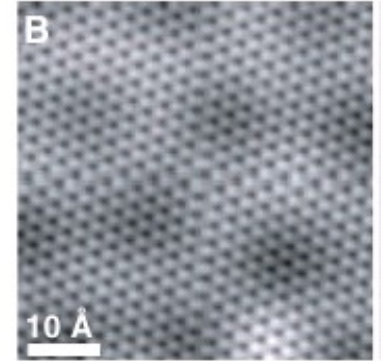
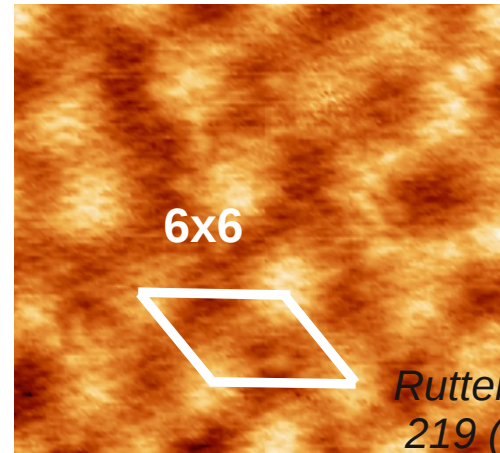
S. Latil et al., Phys. Rev B76, 201402(R) (2007)

second C layer = graphene with soft ripples

Ab initio

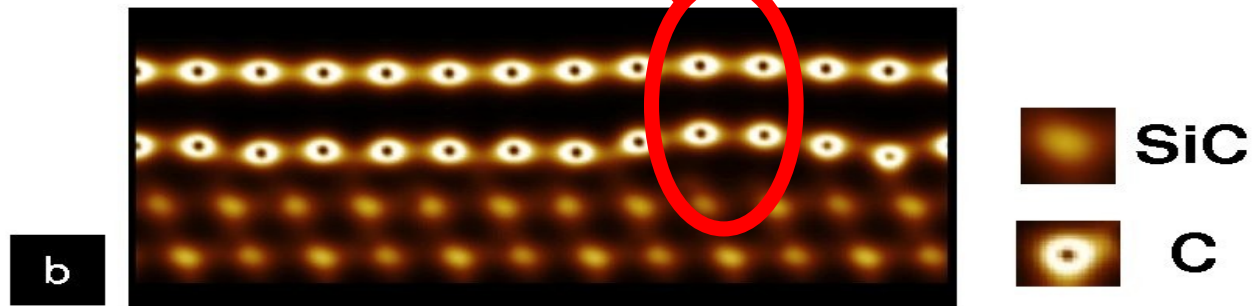


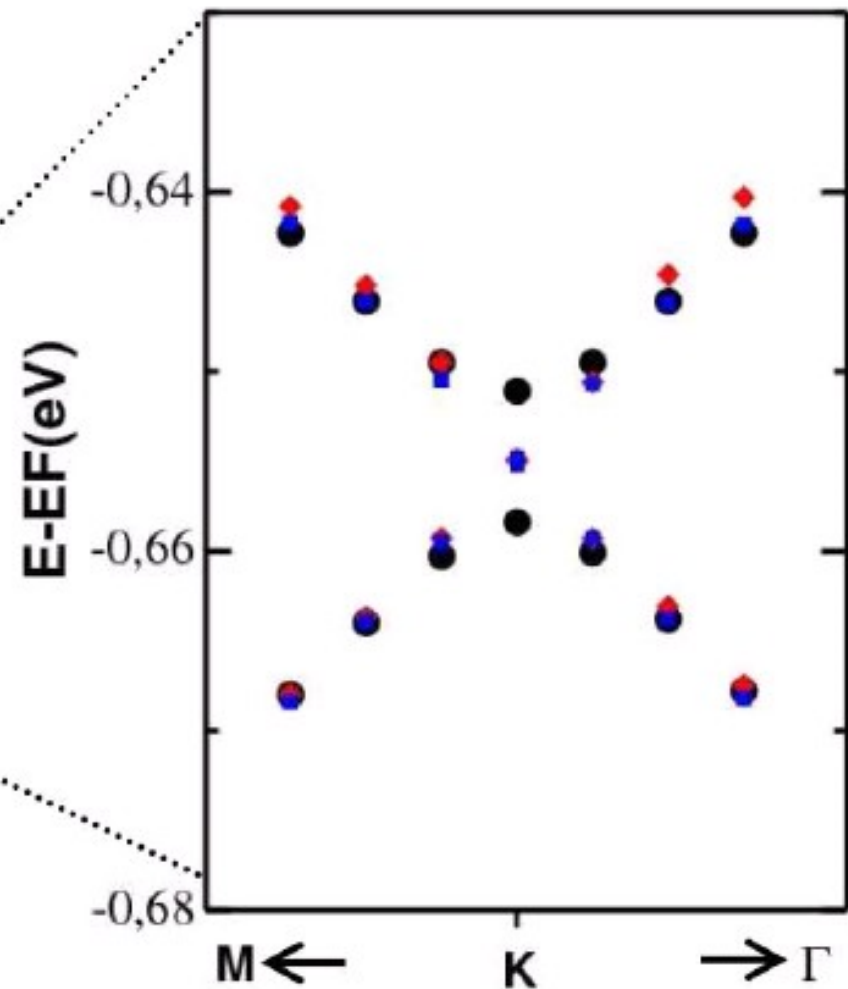
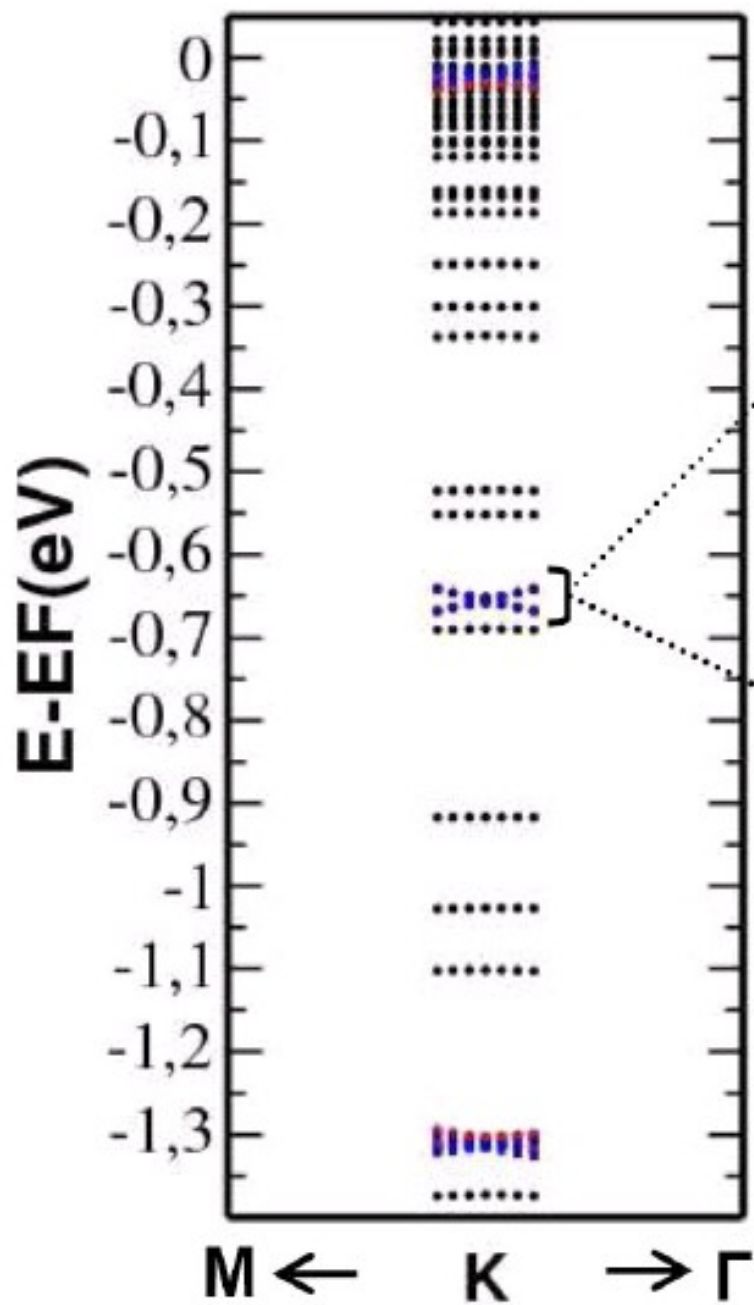
STM image (0.2 V, 300 K),
P.Mallet et al., Phys Rev B74, 041403 (R) (2007)



Rutter et al Science 317, 219 (2007)

Corrugation : 0.5 Å (STM : 0.2 – 0.4 Å), roughly follows buffer layer geometry, generates soft 6x6 ripples
no C-C bond
graphene decoupled from the substrates thanks to the buffer layer

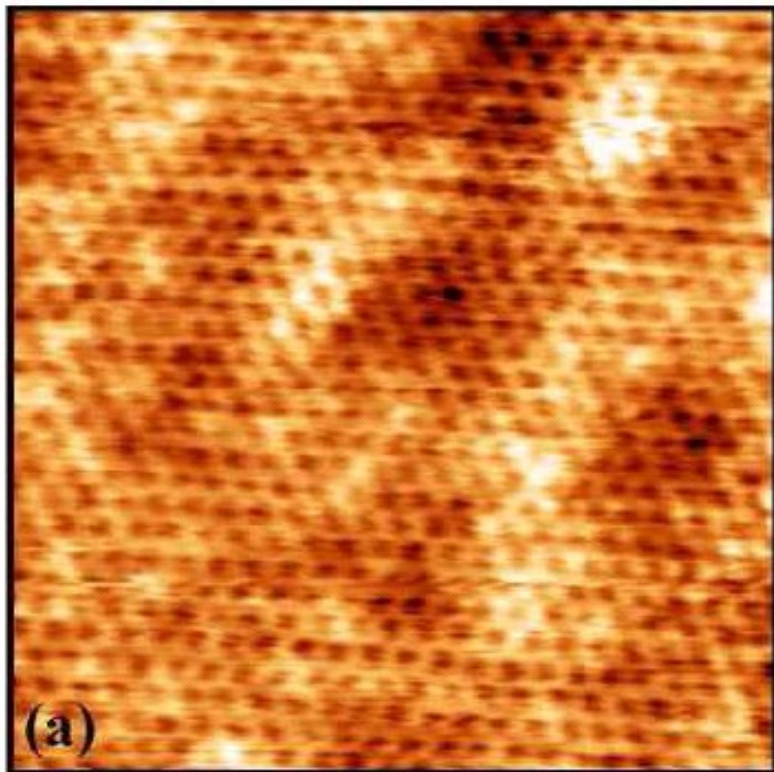




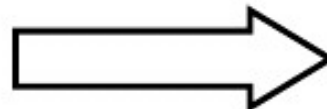
- 6R3 complete calculation
- ◆ Doped monolayer
- Monolayer with ripples

6R3 = complex model but actual interface even more complex

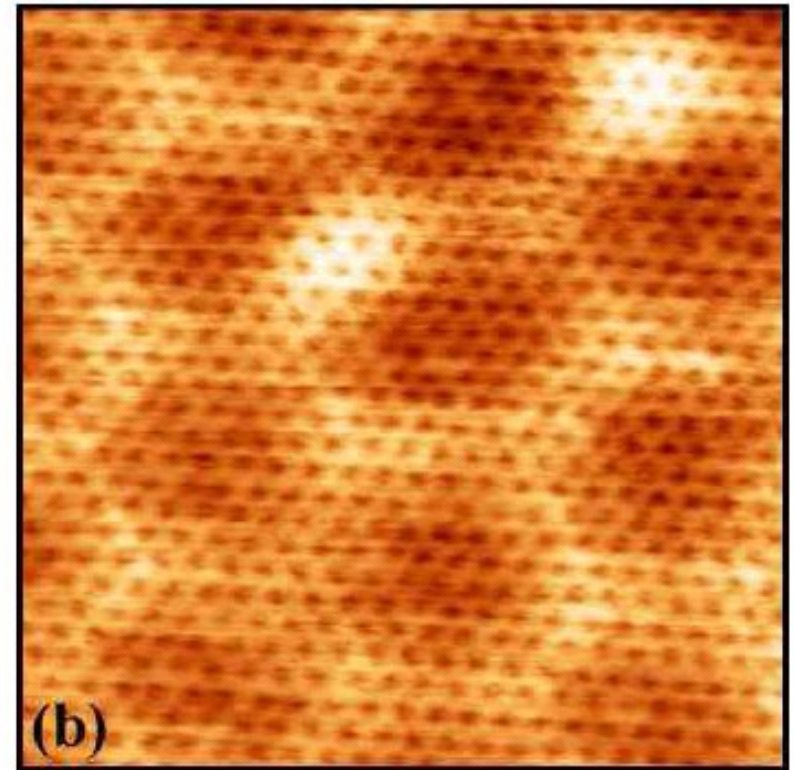
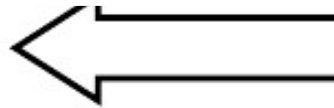
**disorder
adatoms at interface**



Change in tip

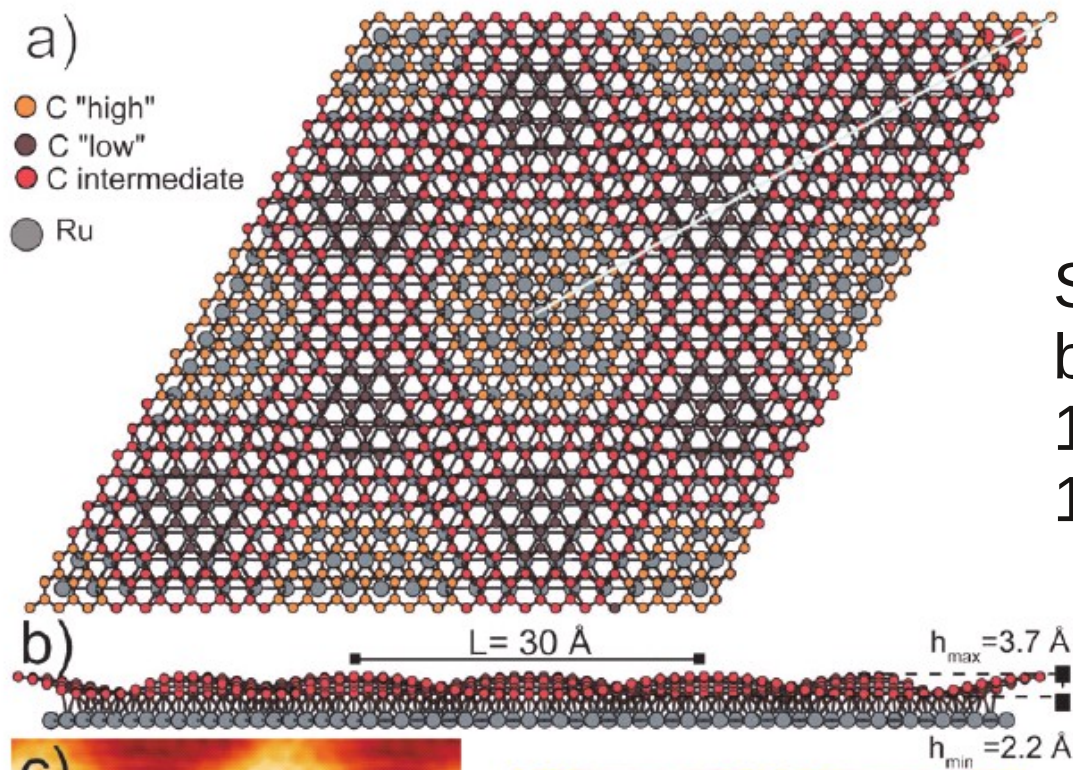


Same
position

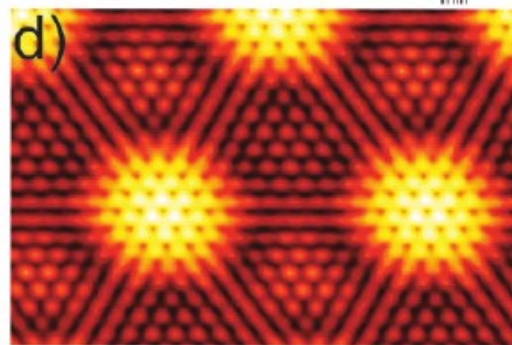
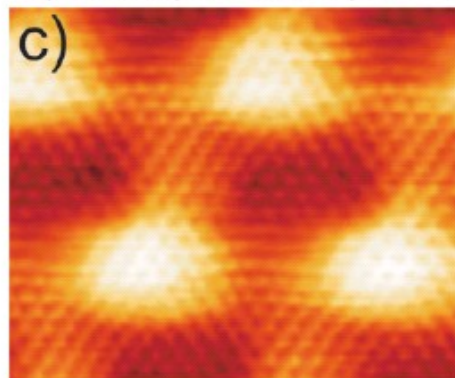


5.6 x 5.6 nm², +0.2 V

Graphene on Ru (0001)



Strong coupling
bufferlayer
12x12 C on
11x11 Ru



Ab initio

STM

1mA, -0.05V

50x40 Å

Marchini et al PRB 76, 075429 (2007)

Wang et al, Phys. Chem. Chem. Phys. 10,
3530 (2008)